## CS1110

## Lecture 11: Intro to Recursion

| Prelim preparation/upcoming schedule |
| :---: |
| This week (Feb 25 - Mar 1) |

Today: lecture (recursion) as usual, plus:

- Prelim conflicts (makeup requests) at midnight on CMS
- A3 out today; short, designed to help prepare you for the exam
Labs today and tomorrow:
- Lab 5 (lists) due
- pick up your graded A2s - feedback will help you for prelim
- Lab 6 (recursion) out - not optional, but that material is not on
the prelim. Due at beginning of lab session after the prelim.
Thursday: lecture (recursion II) as usual
Slides by D. Gires, L. Lee, S. Marschner, W. White
[
.


## Nested Lists (appear in A3)

- Lists can hold any objects
- Lists are objects
- Therefore lists can hold other lists!

$$
\begin{aligned}
& \mathrm{a}=[\text { 'j', 'k'] } \\
& \mathrm{b}=[3,6] \\
& \mathrm{c}=[\text { 'A', 'B', b] } \\
& \mathrm{x}=[7, \mathrm{a}, \mathrm{c}, 5]
\end{aligned}
$$


$x=\left[7,\left[{ }^{\prime} ',{ }^{\prime} \mathrm{k}^{\prime}\right],\left[{ }^{\prime} \mathrm{A}^{\prime}\right.\right.$ ', 'B', $\left.\left.[3,6]\right], 5\right]$


## How to Think About Recursive Functions

1. Have a precise function specification.
2. Base case(s):
" When the argument values are as "small" as possible
When the answer is determined with little calculation
3. Recursive case(s):

- Verify recursive cases with the specification

4. Termination:

- Arguments of calls must somehow get "smaller", so each recursive call gets closer to a base case


## Understanding the String Example

[^0]
## A Recursive Function

```
def num_es(s):
    """Returns: number of 'e's in s. Precond: s a string"""
        if s == ": # case: s is empty string
        return 0
    # case: <s> has at least one char
    return ((l if s[0] == 'e'
else 0) +
num_es(s[l:]))
```

Indeed, if $s$ has at least one character, the number of 'e's in $s$ is the number of 'e's in $s[0]+$ the number of 'e's in $s[1:]$.

## Understanding the String Example

- Step 1: Have a precise specification def num_es(s)
"""Returns: number of 'e's in s. Precond: s a string"""
\# case: s is empty string
if $\mathrm{s}==$ ": $\quad$ Base case
return 0

\# case: s has at least one char
\# return \# of 'e's in s[0]+\# of 'e's in s[1:]
return ( 1 if $\mathrm{s}[0]==$ 'e' else 0 ) + num_es( $\mathrm{s}[1:])$
Recursive case
- Step 2: Check the base case
- When s is the empty string, 0 is returned. Good.


## Example: Remove Blanks from a String

```
def deblank(s):
"""Returns: s with blanks removed"""
if s== "
    return s
# case: s is not empty
if s[0] in string.whitespace:
    return deblank(S[1:])
# case: s not empty and s[0] not blank
return (s[0] +
        deblank(s[l:]))
```

- Check the four points:

1. Precise specification?
2. Base case: correct?
3. Recursive case: progress toward termination?
4. Recursive case: correct?

Expression: x in thelist returns True if $x$ is a member of list thelist (and False if it is not)


[^0]:    - Step 3: Recursive calls make progress toward termination def num_es(s): $\longleftarrow$ parameter s
    ""n"Returns: \# of 'e's in s""I"
    \# $\{\mathrm{s}$ is empty $\}$
    if $s==$ ":
    return 0
    argument $\mathrm{s}[1:]$ is smaller than parameter s , so there is progress toward reaching base case 0
    \# \{ s at least one char \}
    argument s[1:]
    \# return \# of 'e's in s[0]+\# of 'e's in s[1:]
    argument $\mathrm{S}[1:]$
    return ( 1 if $\mathrm{s}[0]==$ 'e' else 0 ) + num_es(s[l:])
    - Step 4: Recursive case is correct

    Just check the specification

