## CS1110

## Lecture 22: Prelim 2 Review Session

## Announcements

Processed prelim regrade requests: on the front table.

## Reminders:

Exam: 7:30-9:00PM, Tuesday Apr $16^{\text {th }}$ Kennedy 116 (Call Auditorium, same as before). Arriving early recommended.

Next Tuesday: lectures replaced by professor office hours in Thurston 102; and labs are staff office hours. Next Wed-Fri: all labs, staff and consulting hours canceled.

We will start (and, we hope, finish) grading Thursday evening/night.

## Material emphasized

Recursion (A4, Lab 6)
Defining and using classes (A4, A6, Lab 8)
For- and while-loops (A4, A6, Lab10)
Code development from invariants (A6, Lab10)
[We will assume knowledge of the material covered previously, in the sense that you should know how to, say, create lists, draw folders and frames, manipulate strings, make appropriate test cases. and so on. This shouldn't require additional studying.]

Hint: re-read spec after doing problem.

## Additional sources of practice problems

- Fall 2012 Prelim 2, questions 4, 5.
- Fall 2012 Final questions, questions 4, 6, 7 given the invariant for insertion sort and the helper function push_down.
- The worked exercises on loop invariants
- Loop problems at http://codingbat.com/python (interactive programming exercises). You can try solving the problems via both loops and recursion, often.


## Provide a recursive implementation

## def merge(sl,sk):

"""Returns: string of characters of sl and sz, in alphabetical order.
Examples: merge('ab', ") = 'ab'
merge('abbce', 'cdg') = 'abbccdeg'
Precondition: sl a string with characters in alphabetical order
s2 a string with characters in alphabetical order"""
if $\mathrm{sl}==$ " or s ==":
return sl + sk
if sl[0] <= s2[0]: \# Pick first from sl and merge the rest return sl[0]+merge(sl[1:],sఓ)
else:
\# Pick first from s2 and merge the rest
return s2[0]+merge(sl,s2[1:])

## Provide a recursive implementation

## def skip(s):

"""Returns: copy of string s, odd letters(i.e., $\left.1^{\text {st }}, 3^{\text {rd }}, 5^{\text {th }}\right)$ dropped.
Example: 'abcd' -> 'bd'. " -> " 'abc' -> 'b', 'zzz' -> 'z' """
if len(s) <= l: \# One base case
return "
else: \# s >= 2 characters (if exactly 2 , another base case)
return $\mathrm{s}[1]+(\operatorname{skip}(\mathrm{s}[2:])$ if len(s) > 2 else ")

## Provide a for-loop implementation

## def skip(s):

"""Returns: copy of string s, odd letters(i.e., $\left.I^{\text {st }}, 3^{\text {rd }}, 5^{\text {th }}\right)$ dropped. Example: 'abcd' -> 'bd'. " -> " 'abc' -> 'b', 'zzz' -> 'z' """
out = " \# progress towards output
\# Inv: chars s[0..i-1] have been processed. Done when i is len(s) for i in range(len(s)):

$$
\begin{aligned}
& \text { if (i } \% 2=1 \text { ): } \\
& \text { out }+=\mathrm{s}[\mathrm{i}]
\end{aligned}
$$

return out

## Provide a while-loop implementation

## def $\operatorname{skip(s):~}$

"""Returns: copy of string s, odd letters(i.e., $\left.1^{\text {st }}, 3^{\text {rd }}, 5^{\text {th }}\right)$ dropped. Example: 'abcd' -> 'bd'. " -> " 'abc' -> 'b', 'zzz' -> 'z' """
out = " \# progress towards output
if len(s) <=1: \# actually these two lines are optional
return out
$\mathrm{i}=1$
\# Inv: chars s[0..i-1] have been processed. Done when $i$ is len(s)
while ( $\mathrm{i}<\operatorname{len}(\mathrm{s})$ ):
out += s[i]
i $+=2$
return out

## Defining a class

## class Paper(object):

"""An instance is a scientific paper.
Class variables:
number [int]: number of papers that have been created. >= 0

Instance variables:
title [string]: title of this paper. At least one char long.
cites [list of Papers]: papers that this book cites
cited_by [list of Papers]: papers that this paper is cited by
|| || ||
number $=0$ \# initial value is 0

## def __init__(self, title, cites=None):

"""Initializer. A new paper with title <title>, citing the papers in list <cites> (set to [] if <cites> is None), and with cited_by set to []. Unlike in A4, this initializer should also update the relevant attributes of any papers in the list <cites>. Pre: arg values as in class specification.
Don't forget to update the class variable. """

## Write the body of __init

## def __init__(self, title, cites=None):

\# spec on previous slide
self.title $=$ title
self.cites $=$ ([] if cites is None else cites)
for $p$ in self.cites:
p.cited_by.append(self)
self.cited_by = []

Paper.number += 1 \# note how to reference the class variable.

## Implement according to invariant

- Given a sequence $b[h . . k]$ with some value x in $\mathrm{b}[\mathrm{h}]$ :

- Swap elements of $b[h . . k]$ and store in i to truthify post:


|  | i j |  |  |  | k |
| :---: | :---: | :---: | :---: | :---: | :---: |
| inv: b | <= x | x | ? | >= x |  |

## Partition Algorithm Implementation

```
def partition(b, h, k):
    """Partition list b[h..k] around a pivot \(\mathrm{x}=\mathrm{b}[\mathrm{h}]\) """
    \(\mathrm{i}=\mathrm{h} ; \mathrm{j}=\mathrm{k}\)
    \# invariant: b[h..i-l] < b[i], b[j+l..k] >= b[i]
    while i < j :
        if \(\mathrm{b}[\mathrm{i}+\mathrm{l}]>=\mathrm{b}[\mathrm{i}]\) :
            \# Move to end of block.
            \(b[i+1], b[j]=b[j], b[i+1]\)
            \(j=j-1\)
        else: \#b[i+1] < b[i]
            \(b[i], b[i+1]=b[i+1], b[i]\)
            \(\mathrm{i}=\mathrm{i}+\mathrm{l}\)
    \# post: \(\mathrm{b}[\mathrm{h} . \mathrm{i}-\mathrm{l}]<\mathrm{x}, \mathrm{b}[\mathrm{i}]\) is x , and \(\mathrm{b}[\mathrm{i}+\mathrm{l} . \mathrm{k}]>=\mathrm{x}\)
    return i
```

def evaluate( $\mathrm{p}, \mathrm{x}$ ): """Returns: The evaluated polynomial $\mathrm{p}(\mathrm{x})$. We represent polynomials as a list of floats:

$$
[1.5,-2.2,3.1,0,-1.0] \text { is } 1.5-2.2 x+3.1 x^{* *} 2+0 x^{* *} 3-x^{* *} 4
$$

We evaluate by substituting in for the value $x$. For example
evaluate([1.5,-2.2,3.1,0,-1.0], 2) = 1.5-2.2(2)+3.1(4)-1(16)=-6.5

$$
\text { evaluate }([2], 4)=2
$$

Precondition: p is a list (len $>0$ ) of floats, x is a float"""

## One implementation

## def evaluate $(p, x)$ :

```
"""(spec on previous slide)"""
    sum = 0 # sum of all the coeffs*x**y for coeffs seen so far
    xval = l # value to multiply with next coeff yet unseen
    for c in p: # c is next unseen coefficient
\[
\begin{aligned}
& \text { sum }=\operatorname{sum}^{+} c^{*} \text { xval } \\
& \text { xval }=\text { xval }^{*} \mathrm{x}
\end{aligned}
\]
return sum
```


## Alternate implementation

def evaluate $(p, x)$ :
"""(spec on previous slide)"""
$\mathrm{i}=0$; xval = l; sum = p[i] \# no point in multiplying by l; showing \# i for clarity; it's not really necessary here
$\mathrm{i}=1$
while i < len(p):

$$
\begin{array}{ll}
\text { \# Invariant: xval }=x^{* *}(i-1) ; \text { sum }=\operatorname{eval}(p[. . i-1], x) \\
\text { xval } *=x & \# \text { or, } x v a l=x v a l * x \\
\text { sum }+=p[i]^{*} \text { xval } & \text { \# or, sum }=\operatorname{sum}+p[i]^{*} \text { xval } \\
i+=1 & \# \text { or, } i=i+1
\end{array}
$$

return sum

