

Support Vector Machines and Optimal Hyperplanes

CS6780 – Advanced Machine Learning Spring 2019

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Reading: Murphy 14.5 Schoelkopf/Smola Chapter 5 (rest), Chapter 7.1-7.3, 7.5







Vapnik Chervonenkis Dimension

 Definition: The VC-Dimension of H is equal to the maximum number d of examples that can be split into two sets in all 2^d ways using functions from H (shattering).



VC Dimension of Hyperplanes

- Theorem: The VC Dimension of unbiased hyperplanes over N features is N.
- Theorem: The VC Dimension of biased hyperplanes over N features is N+1.

VC Dimension of
Margin HyperplanesTheorem: Unbiased linear classifiers H_X with
 $||w|| = 1/\delta$ and $\max_i ||x_i|| \le R$ and margin
 $\min_i |w \cdot x_i| = 1$ $\min_i |w \cdot x_i| = 1$ for a given set of instances $X = \{x_1, \dots, x_k\}$,
have VC DimensionVCDim $(H_X) \le \frac{R^2}{\delta^2}$