Shell Texture Function

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Introduction

 Problem: appearance of non-homogeneous object with surface mesostructures is complex.



Introduction

- First observation: deep within a volume, radiance exhibits an averaging effect of the material properties.
- Second observation: contribution of light from deep within a volume to the appearance of an object is small.

Introduction

- Idea: split the volume into a heterogeneous shell layer with surface mesostructures and a homogeneous inner core.
- Precompute the non-homogeneous shell layer.
- Simulate the homogeneous inner core with dipole diffusion approximation.



- STF representation
- Construction of STF sample
- Shell synthesis
- STF rendering
- Results

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- STF base volume: array of voxels on a regular 3D grid.
- For subsurface voxels x, store extinction coefficient $\kappa(x)$, albedo $\alpha(x)$, and phase function $f(x, \omega', \omega)$.
- For surface voxels, store surface normal and relative index of refraction as well.

• Light transport in participating medium: $(\boldsymbol{\omega} \cdot \nabla)L(x, \boldsymbol{\omega}) = \sigma_a(x)L_e(x, \boldsymbol{\omega}) + \sigma_s(x)L_i(x, \boldsymbol{\omega}) - \kappa(x)L(x, \boldsymbol{\omega})$

 Compute in-scattered radiance using volume photon mapping [Jensen and Christensen 1998]:

$$L_i(x, \mathbf{\omega}) = \frac{1}{\sigma_s(x)} \sum_{p=1}^n f(x, \mathbf{\omega}_p, \mathbf{\omega}) \frac{\Delta \Phi_p(x, \mathbf{\omega}_p)}{\Delta V}$$

- Divide flux into single-scattering and multiple-scattering terms.
- Multiple scattering can be considered approximately isotropic [Stam 1995]; therefore:

$$L_{i}(x, \omega) = f(x, \omega_{l}, \omega) \frac{\sum_{s} \Delta \Phi_{p}(x, \omega_{l})}{\sigma_{s}(x) \Delta V} + \frac{1}{4\pi} \frac{\sum_{m} \Delta \Phi_{p}(x, \omega_{p})}{\sigma_{s}(x) \Delta V}$$
$$L_{i}(x, \omega) = f(x, \omega_{l}, \omega) I_{s}(x, \omega_{l}) + \frac{1}{4\pi} I_{m}(x, \omega_{l})$$

• STF is a 5D function with single-scattering component $I_s(x, \omega_l)$ and multiple-scattering component $I_m(x, \omega_l)$.

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Acquisition of base volume

 Two ways to obtain base volume: measure real materials or scan convert existing 3D models.

Acquisition of base volume

- For measured volume data, base volume is created using voxel classification [Kaufman 1991].
- In scan conversion, scan algorithm determines the material in each voxel.

Acquisition of base volume

- For each material, obtain its extinction coefficient and albedo from published measurement tables.
- Use Henyey-Greenstein phase function.

STF irradiance sampling

- Emit photons along a light direction ω_l and evaluate their contributions to the STF.
- Each time a photon p interacts with the medium at voxel x, add its contribution to $I_s(x, \omega_l)$ if it is p's first interaction, or to $I_m(x, \omega_l)$ otherwise.

STF irradiance sampling

• Backlighting arrives from the homogeneous inner core and multiple-scattering STF values for all directions are averaged and recorded as $I_m(x, \omega_b)$.



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Object shell synthesis

- Regard the base volume as a 2D texture, where each texel consists of a stack of voxels.
- Synthesize the texture onto the target surface mesh using the algorithm proposed by Tong et al. [Tong et al. 2002].











(C)

Shell resampling

- Resulting shell is a dense set of points on an irregular grid.
- Resample these points onto a regular grid to facilitate subsequent rendering operations.



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STF rendering

- Radiance L(x,w) of a surface voxel xtoward viewing direction ω is as follows. $L(x,\omega) = (1 - F_t)L_R(x,\omega_r) + F_tL_T(x,\omega_t)$
- $L_R(x, \omega_r)$ is evaluated by conventional ray tracing. $L_T(x, \omega_t)$ is evaluated as follows.

$$L_T(x, \mathbf{\omega}_t) = \int_{x_0}^x \sigma_s(x') e^{-\int_{x'}^x \kappa(\xi) d\xi} I_b(x', \mathbf{\omega}_t) dx'$$

STF rendering

• $I_b(x', \omega_t)$ is computed as follows.

$$I_b(x', \omega_t) = \frac{1}{4\pi} I_0(x'_l, \omega_l) I_m(x', \omega_l) + \frac{1}{4\pi} L_d(x'_d, \omega_l) I_m(x', \omega_b) + \frac{1}{4\pi} L_d(x'_d, \omega_b) + \frac{1}{4\pi} L_d(x'_d, \omega_b) I_m(x', \omega_b) + \frac{1}{4\pi} L_d(x$$

 $f(x', \boldsymbol{\omega}_l, \boldsymbol{\omega}_t) I_0(x'_l, \boldsymbol{\omega}_l) I_s(x', \boldsymbol{\omega}_l)$

STF rendering

- The first two terms account for isotropic multiple scattering from voxels within the shell. The value of $L_d(x'_d, \omega_l)$ is obtained from dipole diffusion approximation.
- The third term accounts for single scattering that is reflected in direction ω_t .



Figure 6: Ray tracing geometry.

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