Organization

1. Optimal Representation of Control dependence

- Definition
- Is the control dependence graph (O(|E|*|V|) space/time) optimal?

2. Our approach:

- Reduce problem to ROMAN CHARIOTS PROBLEM
- Build **APT** data structure in O(|E| + |V|) space/time
- => **APT** is an optimal representation of control dependence

3. Other applications of APT:

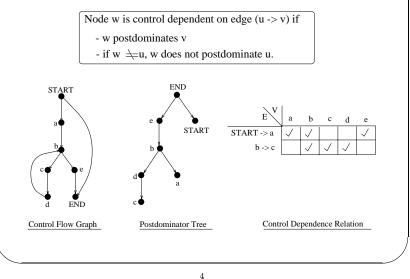
- SSA computation in linear time per variable
- SDEG computation in linear time per problem
- DFG computation in linear time per variable

4. Conclusions:

- **APT** is a factored form of the CDG which requires 'filtered search' to answer queries

2

Control dependence: (Ferrante, Ottenstein, Warren 1987)



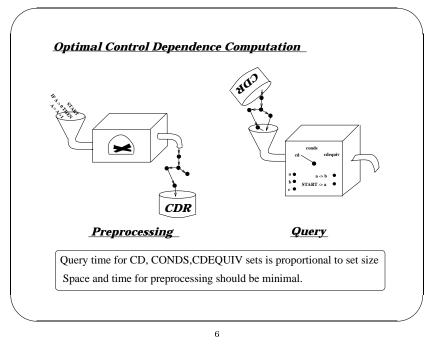
Control Dependence, Program Analyses and The Roman Chariots Problem

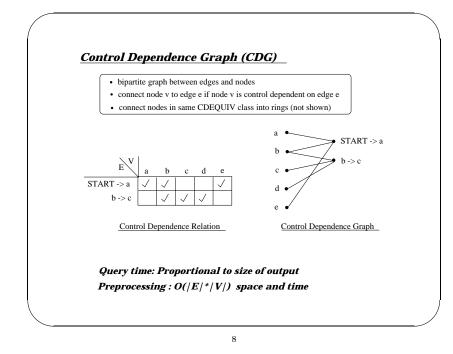
> Keshav Pingali Cornell University

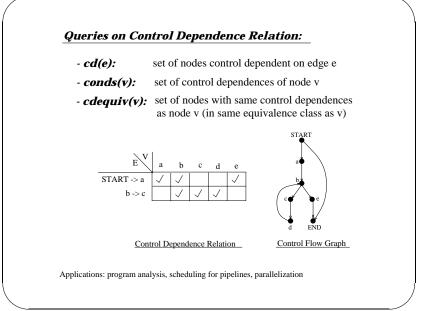
Gianfranco Bilardi Universita di Padova, Italy

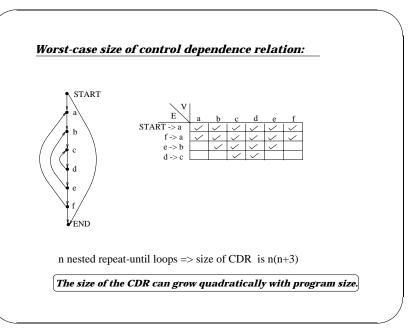


What is an Optimal Representation of Control Dependence?









Part II:

APT

and the

Roman Chariots Problem

10

There have been many unsuccessful efforts to reduce the size of the CDG.

"We therefore conjecture that to enumerate [conds sets] in time proportional to [the size of the set] requires a data structure of quadratic size."

[Cytron,Ferrante,Sarkar, PLDI 1990]

Key Idea (I): Exploit structure of relation

Analogy: Postdominator relation

- queries: immediate pdom of node, all pdoms of node
- size of relation is $O(|V|^2)$

- relation is transitive, so build transitive reduction (pdom tree) in O(|E|) time [Harel,Tarjan]

- query time using pdom tree is optimal

=> There is no point in constructing the entire relation

What structure is there in the control dependence relation?

Control dependence relation:

nodes that are control dependent on an edge e form a simple path in the postdominator tree
in a tree, a simple path is uniquely specified by its endpoints

Postdominator tree + endpoints of each control dependence path can be built in O(/E/) space and time

12

Our Solution:

- reduce control dependence computation to a graph problem called *Roman Chariots Problem*
- design a data structure called **APT** (augmented postdominator tree)

(a) which can be built in O(|E|) space and time, and
(b) which can be used to answer CD,CONDS and CDEQUIV queries in time proportional to output size.

APT is a data structure for optimal control dependence computation.

How can we use the compact representation of the CDR to answer queries for CD,CONDS and CDEQUIV sets in time proportional to output size?

<u>CD(n): Which cities are served by chariot n?</u>

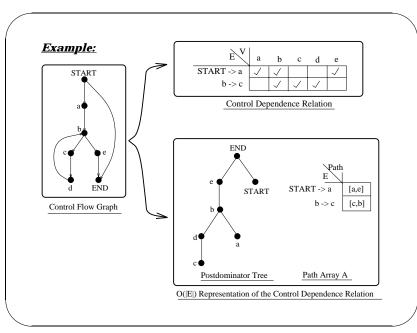
Query procedure: (similar to FOW 87)

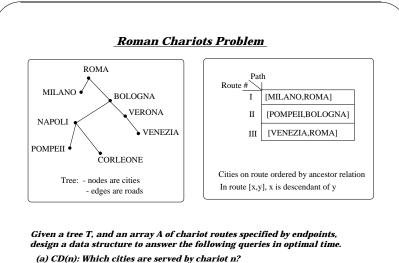
- Look up entry for chariot n in Route Array (say it is [x,y])
- Traverse nodes in tree T, starting at x and ending at y
- Output all nodes encountered in traversal

(cf. CDG: many routes can share tree nodes/edges)

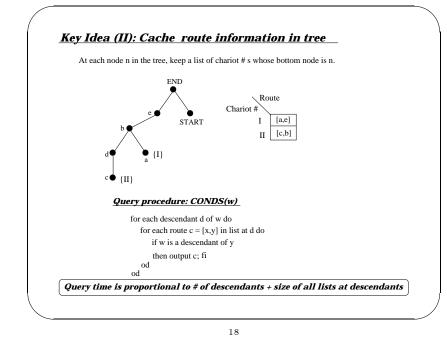
CD query time is proportional to output size.

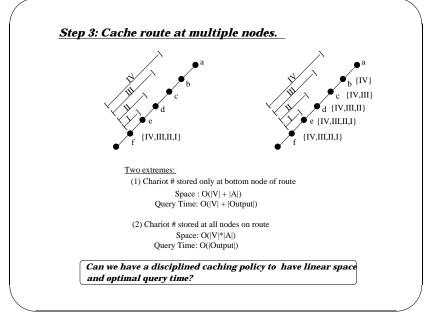


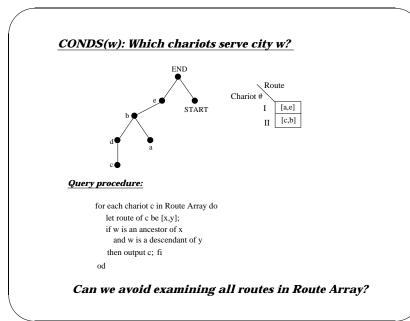


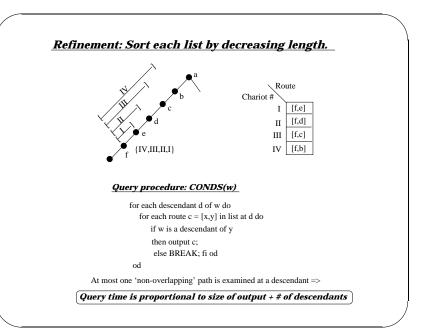


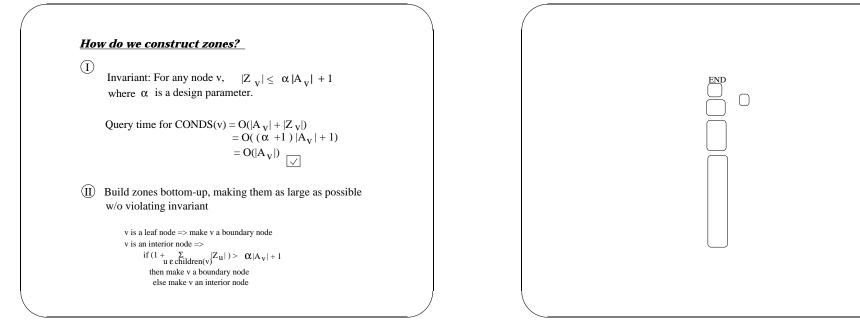
- (b) CONDS(w): Which chariots serve city w?
- (c) CDEQUIV(w): Which cities are served by the same chariots that serve w?

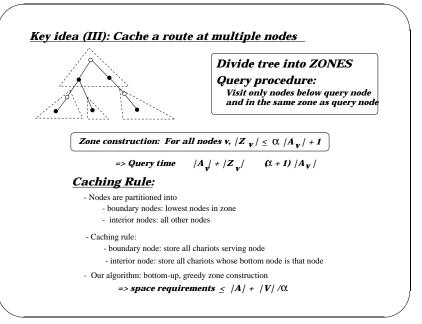


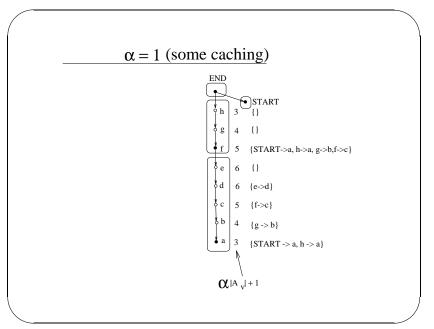




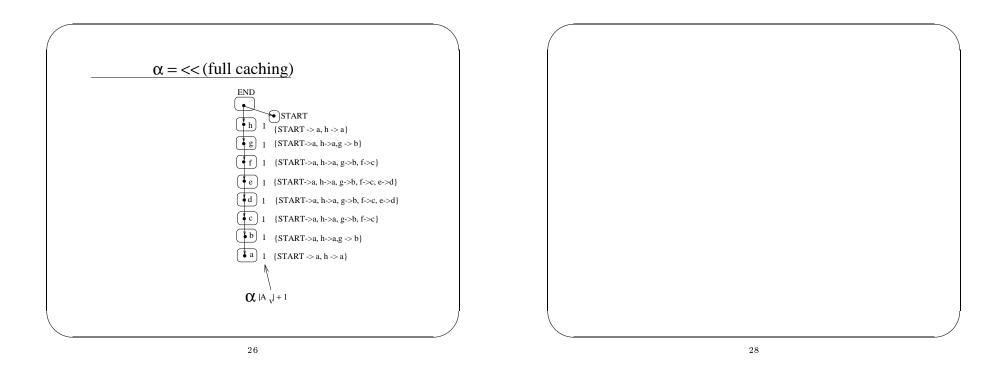


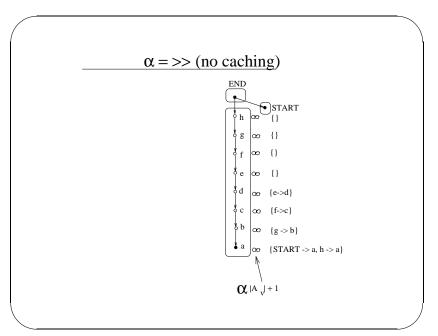


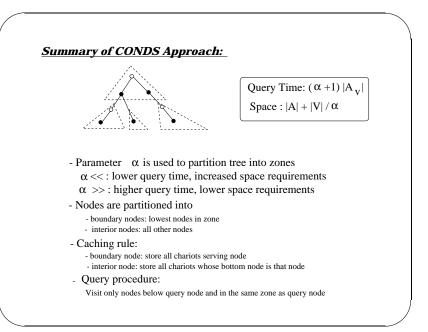


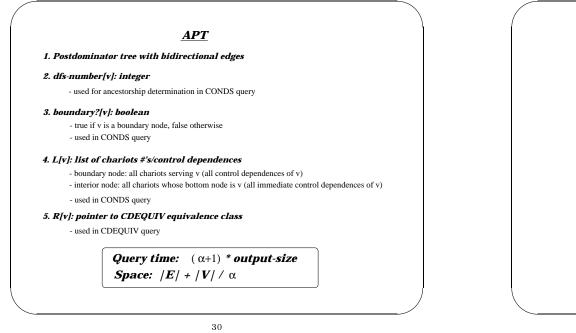


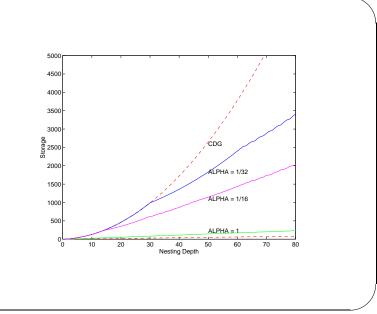
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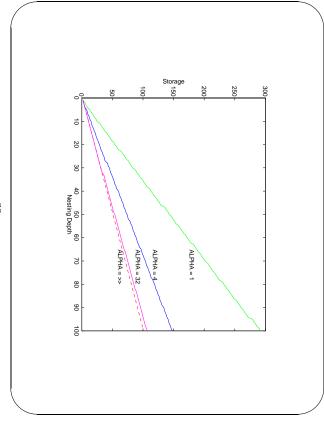


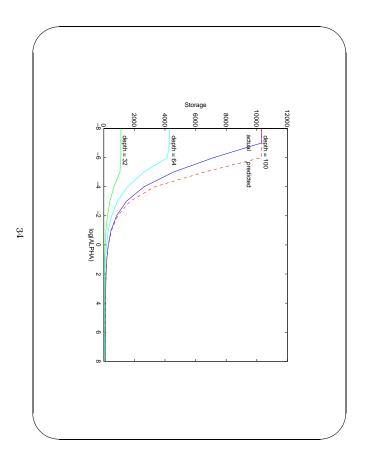


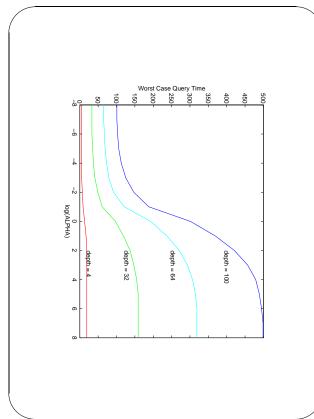
CDEQUIV(v): Which cities are served by same chariots that serve v? • Ferrante, Ottenstein, Warren 87: $O(|E|^{3})$ using hashing for set equality • Cytron, Ferrante, Sarkar 90: $O(|E|^{2})^{2}$ • Ball 92: O(|E|) for structured programs • Podgurski 93: O(|E|) for forward control dependence in general graphs • Johnson, Pearson, Pingali 94: O(|E|) for general graphs (optimal) **DEEQUIV for Roman Chariots Problem** • cleaned-up version of JPP94 algorithm • compute two finger prints for CONDS sets • size of CONDS set • Lo:lowest node contained in all routes of CONDS set $f_{D} = \frac{1}{2} \int_{0}^{1} \int_{0}^{1} \int_{0}^{1} \int_{0}^{1} \int_{0}^{1} (CONDS(a)) = a \\ Lo(CONDS(d)) = f \\ Lo(CONDS(e)) = f \\ Lo(CONDS) = f \\ Lo(CON$

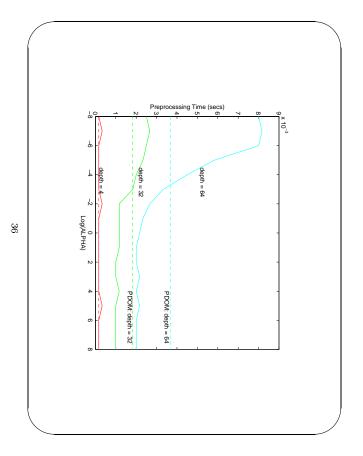
<u>Experimental Results</u>

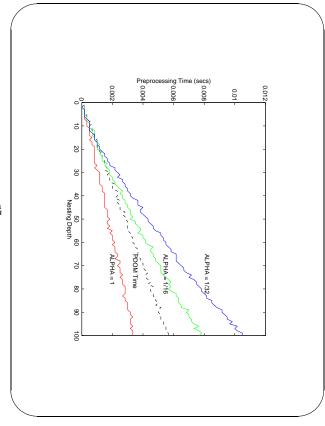
Can compute finger-prints in O(|V| + |A|) space and time

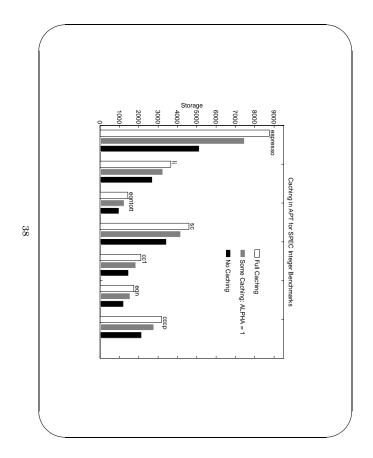


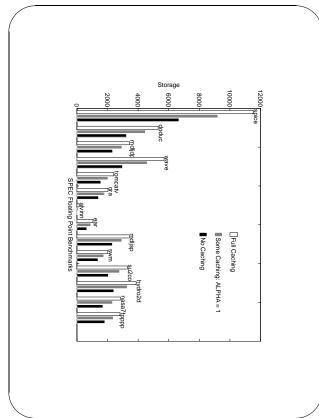


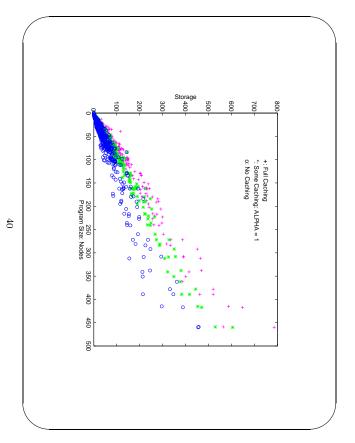


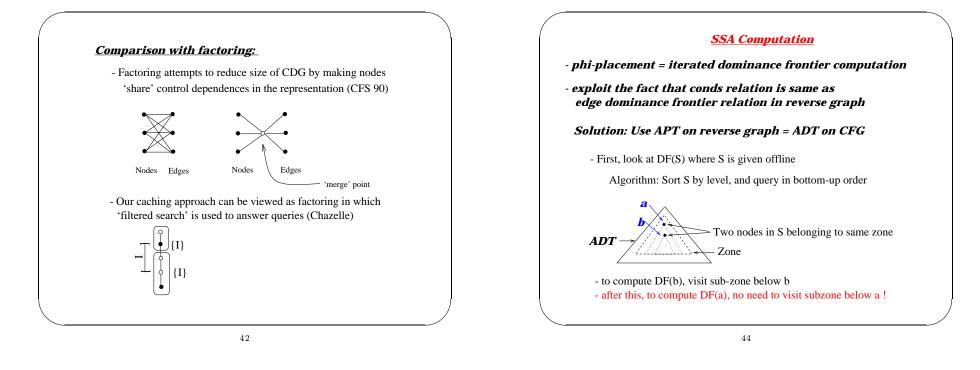


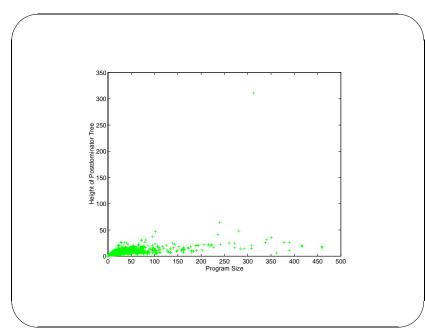


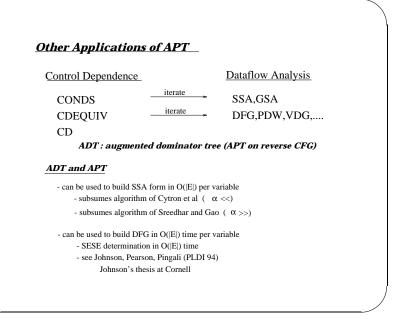


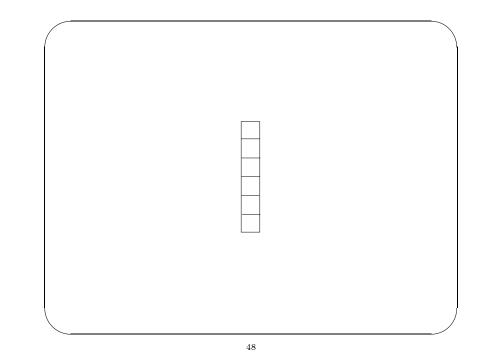










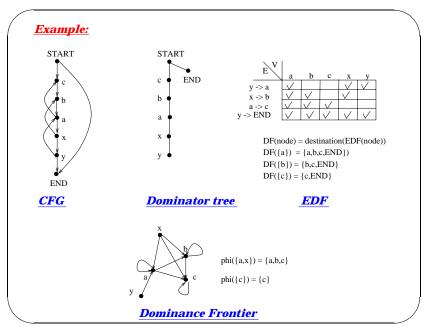


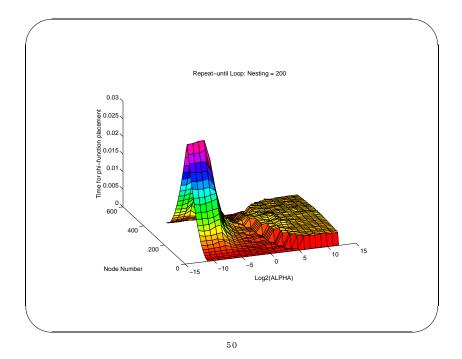
<u>Algorithm:</u>

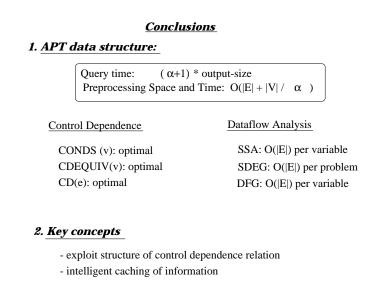
- Sort nodes in S by level.
- Remove nodes from sorted list by decreasing level order, and query in *ADT*
- After a node is queried, mark it in **ADT** so further queries that reach v do not look below v.
- **Time = O(|V| + |A|)** (O|E|) in CFG terms

What if set for querying is given online?

- We can use same strategy provided nodes are presented for querying in bottom-up order.
- Happily, if n is in DF(m), then level(n) <= level(m) !!
- => use a priority queue for 'dynamic sorting'
 - Priority queue implementation: (k = # of keys = height of ADT)
 - van Emde Boas: O(log(log(k))) per insertion and deletion
 - Sreedhar and Gao: use an array of size k







Remarks:

- Time to build SSA form: O(|E|) per variable
- Subsumes algorithms of Cytron etal and Sreedhar and Gao
 - $\alpha \ll Cytron et al [91] O(|E|*|V|) per variable$
 - $\alpha \;\; >>$: Sreedhar and Gao (PLDI 95) O(|E|) per variable
- Same idea can be used to build sparse dataflow evaluator graphs for other dataflow problems

- What is best value of α ? Interesting tradeoff

- small value: repeatedly discover that some node is in transitive closure
- large value: time to compute individual DF sets may be large
- intermediate value may be best!

