

CS514: Intermediate Course in Operating Systems

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Recap... Consistent cuts

- On Monday we saw that simply gathering the state of a system isn't enough
- Often the "state" includes tricky relationships
- Consistent cuts are a way of collecting state that "could" have arisen *concurrently in real-time*

What time is it?

- In distributed system we need practical ways to deal with time
 - E.g. we may need to agree that update A occurred before update B
 - Or offer a "lease" on a resource that expires at time 10:10.0150
 - Or *guarantee* that a time critical event will reach all interested parties within 100ms

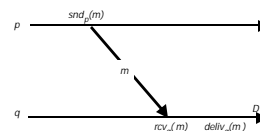
But what does time "mean"?

- Time on a global clock?
 - E.g. with GPS receiver
- ... or on a machine's local clock
 - But was it set accurately?
 - And could it drift, e.g. run fast or slow?
 - What about faults, like stuck bits?
- ... or could try to agree on time

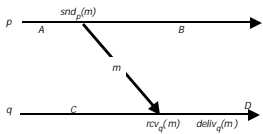
Lamport's approach

- Leslie Lamport suggested that we should reduce time to its basics
 - Time lets a system ask "Which came first: event A or event B?"
 - In effect: time is a means of labeling events so that...
 - If A happened before B, $\text{TIME}(A) < \text{TIME}(B)$
 - If $\text{TIME}(A) < \text{TIME}(B)$, A happened before B

Drawing time-line pictures:

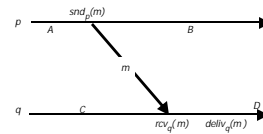


Drawing time-line pictures:



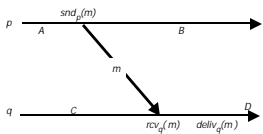
- A, B, C and D are “events”.
 - Could be anything meaningful to the application
 - So are $\text{snd}_p(m)$ and $\text{rcv}_q(m)$ and $\text{deliv}_q(m)$
- What ordering claims are meaningful?

Drawing time-line pictures:



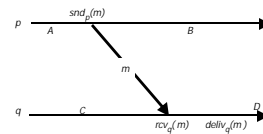
- A happens before B, and C before D
 - “Local ordering” at a single process
 - Write $A \rightarrow^p B$ and $C \rightarrow^q D$

Drawing time-line pictures:



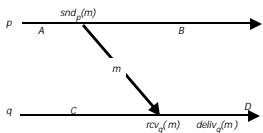
- $\text{snd}_p(m)$ also happens before $\text{rcv}_q(m)$
 - “Distributed ordering” introduced by a message
 - Write $\text{snd}_p(m) \xrightarrow{m} \text{rcv}_q(m)$

Drawing time-line pictures:



- A happens before D
 - Transitivity: A happens before $\text{snd}_p(m)$, which happens before $\text{rcv}_q(m)$, which happens before D

Drawing time-line pictures:



- B and D are concurrent
 - Looks like B happens first, but D has no way to know. No information flowed...

Happens before “relation”

- We’ll say that “A happens before B”, written $A \rightarrow^p B$, if
 1. $A \rightarrow^p B$ according to the local ordering, or
 2. A is a snd and B is a rcv and $A \xrightarrow{m} B$, or
 3. A and B are related under the transitive closure of rules (1) and (2)
- So far, this is just a mathematical notation, not a “systems tool”

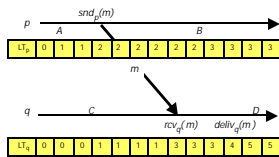
Logical clocks

- A simple tool that can capture parts of the happens before relation
- First version: uses just a single integer
 - Designed for big (64-bit or more) counters
 - Each process p maintains LT_p , a local counter
 - A message m will carry LT_m

Rules for managing logical clocks

- When an event happens at a process p it increments LT_p .
 - Any event that matters to p
 - Normally, also *snd* and *rcv* events (since we want receive to occur "after" the matching send)
- When p sends m , set
 - $LT_m = LT_p$
- When q receives m , set
 - $LT_q = \max(LT_q, LT_m) + 1$

Time-line with LT annotations



- $LT(A) = 1$, $LT(\text{snd}_p(m)) = 2$, $LT(m) = 2$
- $LT(\text{rcv}_q(m)) = \max(1, 2) + 1 = 3$, etc...

Logical clocks

- If A happens before B, $A \rightarrow B$, then $LT(A) < LT(B)$
- But converse might not be true:
 - If $LT(A) < LT(B)$ can't be sure that $A \rightarrow B$
 - This is because processes that don't communicate still assign timestamps and hence events will "seem" to have an order

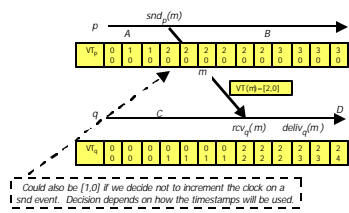
Can we do better?

- One option is to use *vector* clocks
- Here we treat timestamps as a list
 - One counter for each process
- Rules for managing vector times differ from what did with logical clocks

Vector clocks

- Clock is a vector: e.g. $VT(A) = [1, 0]$
 - We'll just assign p index 0 and q index 1
 - Vector clocks require either agreement on the numbering, or that the actual process id's be included with the vector
- Rules for managing vector clock
 - When event happens at p , increment $VT_p[\text{index}_p]$
 - Normally, also increment for *snd* and *rcv* events
 - When sending a message, set $VT(m) = VT_p$
 - When receiving, set $VT_q = \max(VT_q, VT(m))$

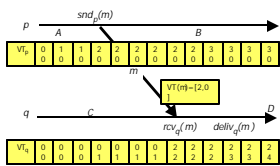
Time-line with VT annotations



Rules for comparison of VTs

- We'll say that $VT_A = VT_B$ if
 - $\forall i, VT_A[i] = VT_B[i]$
- And we'll say that $VT_A < VT_B$ if
 - $VT_A = VT_B$ but $VT_A \neq VT_B$
 - That is, for some $i, VT_A[i] < VT_B[i]$
- Examples?
 - $[2,4] = [2,4]$
 - $[1,3] < [7,3]$
 - $[1,3]$ is "incomparable" to $[3,1]$

Time-line with VT annotations



- $VT(A) = [1,0]$. $VT(D) = [2,4]$. So $VT(A) < VT(D)$
- $VT(B) = [3,0]$. So $VT(B)$ and $VT(D)$ are incomparable

Vector time and happens before

- If $A \rightarrow B$, then $VT(A) < VT(B)$
 - Write a chain of events from A to B
 - Step by step the vector clocks get larger
- If $VT(A) < VT(B)$ then $A \rightarrow B$
 - Two cases: if A and B both happen at same process p, trivial
 - If A happens at p and B at q, can trace the path back by which q "learned" $VT_A[p]$
- Otherwise A and B happened concurrently

Consistent cuts

- If we had time, we could revisit these using logical and vector clocks
- In fact there are algorithms that find a consistent cut by
 - Implementing some form of clock
 - Asking everyone to record their state at time $now + \delta$ (for some large δ)
- And this can be made to work well...

Replication

- Another use of time arises when we talk about replicating data in distributed systems
- The reason is that:
 - We replicate data by multicasting updates over a set of replicas
 - They need to apply these updates in the same order
 - And order is a temporal notion

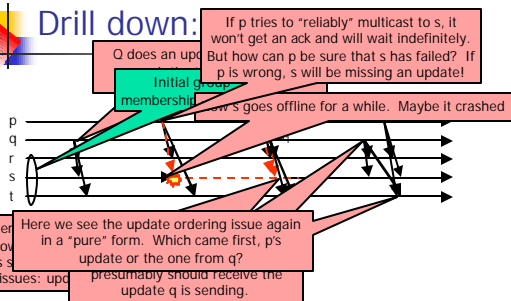
... and replication is powerful!

- Replicate data or a service for high availability
- Replicate data so that group members can share loads and improve scalability
- Replicate locking or synchronization state
- Replicate membership information in a data center so that we can route requests
- Replicate management information or parameters to tune performance

Let's look at time vis-à-vis updates

- Maybe logical notions of time can help us understand when one update comes before another update
- Then we can think about building replicated update algorithms that are optimized to run as fast as possible while preserving the needed ordering

Drill down:



Questions to ask about order

- Who should receive an update?
- What update ordering to use?
- How expensive is the ordering property?

Questions to ask about order

- Delivery order for concurrent updates
 - Issue is more subtle than it looks!
 - We can fix a system-wide order, but...
 - Sometimes nobody notices out of order delivery
 - System-wide ordering is expensive
 - If we care about speed we may need to look closely at cost of ordering

Ordering example

- System replicates variables x, y
 - Process p sends " $x = x/2$ "
 - Process q sends " $x = 83$ "
 - Process r sends " $y = 17$ "
 - Process s sends " $z = x/y$ "
- To what degree is ordering needed?

Ordering example

- $x = x/2$ $x = 83$
- These clearly "conflict"
 - If we execute $x = x/2$ first, then $x = 83$, x will have value 83.
 - In opposite order, x is left equal to 41.5

Ordering example

- $x = x/2$ $y = 17$
- These don't seem to conflict
 - After the fact, nobody can tell what order they were performed in

Ordering example

- $z = x/y$
- This conflicts with updates to x , updates to y and with other updates to z

Commutativity

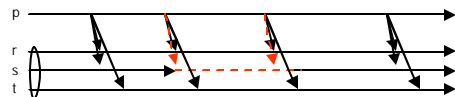
- We say that operations "commute" if the final effect on some system is the same even if the order of those operations is swapped
- In general, a system worried about ordering concurrent events need not worry if the events commute

Single updater

- In many systems, there is only one process that can update a given type of data
 - For example, the variable might be "sensor values" for a temperature sensor
 - Only the process monitoring the sensor does updates, although perhaps many processes want to read the data and we replicate it to exploit parallelism
 - Here the only "ordering" that matters is the FIFO ordering of the updates emitted by that process

Single updater

- If p is the only update source, the need is a bit like the TCP "fifo" ordering



Mutual exclusion

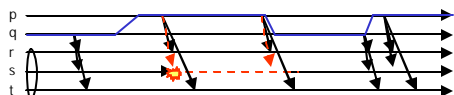
- Another important case we'll study closely
- Arises in systems that use locks to control access to shared data
 - This is very common, for example in "transactional" systems (we'll discuss them next week)
 - Very often without locks, a system rapidly becomes corrupted

Mutual exclusion

- Suppose that before performing conflicting operations, processes must lock the variables
- This means that there will never be any true concurrency
- And it simplifies our ordering requirement

Mutual exclusion

- Dark blue when holding the lock



- How is this case similar to "FIFO" with one sender? How does it differ?

Mutual exclusion

- Are these updates in "FIFO" order?
 - No, the sender isn't always the same
 - But yes in the sense that there is a unique path through the system (corresponding to the lock) and the updates are ordered along that path
- Here updates are ordered by Lamport's happened before relation: →

Types of ordering we've seen

- cheapest* ■ Deliver updates in an order matching the FIFO order in which they were sent
- Still cheap* ■ Deliver updates in an order matching the → order in which they were sent
- More costly* ■ For conflicting concurrent updates, pick an order and use that order at all replicas
- Most costly* ■ Deliver an update to all members of a group according to "membership view" determined by ordering updates wrt view changes

Types of ordering we've seen

- fbcast* ■ Deliver updates in an order matching the FIFO order in which they were sent
- cbcast* ■ Deliver updates in an order matching the → order in which they were sent
- abcast* ■ For conflicting concurrent updates, pick an order and use that order at all replicas
- gbcast* ■ Deliver an update to all members of a group according to "membership view" determined by ordering updates wrt view changes



Recommended readings

- In the textbook, we're at the beginning of Part III (Chapter 14)
- We'll build up the "virtual synchrony" replication model in the next lecture and see how it can be built with 2PC, 3PC, consistent cuts and ordering