

Instance-Based Learning

CS478 – Machine Learning
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Reading: Mitchell Chapter 1 & Sections 8.1 - 8.2

Concept Learning

Definition:

Acquire an operational definition of a general category of objects given positive and negative training examples.

Concept Learning Example

correct (3)	color (2)	original (2)	presentation (3)	binder (2)	A+Homework
complete	yes	yes	clear	no	yes
complete	no	yes	clear	no	yes
partial	yes	no	unclear	no	no
complete	yes	yes	clear	yes	yes

Instance Space X: Set of all possible objects described by attributes (often called features).

Concept c: Subset of objects from X (c is unknown).

Target Function f: Characteristic function indicating membership in c based on attributes (i.e. label)(f is unknown).

Training Data S: Set of instances labeled with target function.

Concept Learning as Learning a Binary Function

- **Task:**
 - Learn (to imitate) a function $f: X \rightarrow \{+1, -1\}$
- **Training Examples:**
 - Learning algorithm is given the correct value of the function for particular inputs \rightarrow **training examples**
 - An **example** is a pair (x, y) , where x is the input and $y=f(x)$ is the output of the target function applied to x .
- **Goal:**
 - Find a function
 - $h: X \rightarrow \{+1, -1\}$
 - that approximates
 - $f: X \rightarrow \{+1, -1\}$
 - as well as possible.

K-Nearest Neighbor (KNN)

- **Given: Training data $(\vec{x}_1, y_1), \dots, (\vec{x}_n, y_n)$**
 - Attribute vectors: $\vec{x}_i \in X$
 - Label: $y_i \in \{-1, +1\}$
- **Parameter:**
 - Similarity function: $K: X \times X \rightarrow \mathbb{R}$
 - Number of nearest neighbors to consider: k
- **Prediction rule**
 - New example x'
 - K-nearest neighbors: k training examples with largest $K(\vec{x}_i, \vec{x}')$

$$h(\vec{x}') = \arg \max_{y \in Y} \left\{ \sum_{i \in k \text{NN}(\vec{x}')} \mathbf{1}_{[y_i=y]} \right\}$$

KNN Example

	correct (3)	color (2)	original (2)	presentation (3)	binder (2)	A+Homework
1	complete	yes	yes	clear	no	yes / +1
2	complete	no	yes	clear	no	yes / +1
3	partial	yes	no	unclear	no	no / -1
4	complete	yes	yes	clear	yes	yes / +1

- **How will new examples be classified?**
 - Similarity function?
 - Value of k ?

$$h(\vec{x}') = \arg \max_{y \in Y} \left\{ \sum_{i \in k \text{NN}(\vec{x}')} \mathbf{1}_{[y_i=y]} \right\}$$

Weighted K-Nearest Neighbor

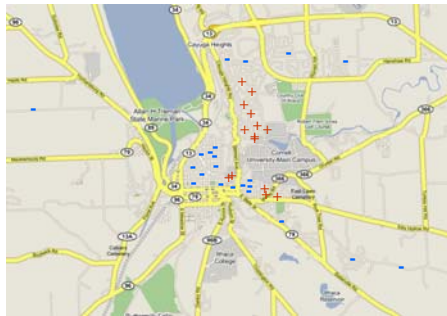
- **Given: Training data** $(\vec{x}_1, y_1), \dots, (\vec{x}_n, y_n)$
 - Attribute vectors: $\vec{x}_i \in \mathcal{X}$
 - Target attribute: $y_i \in \{-1, +1\}$
- **Parameter:**
 - Similarity function: $K : \mathcal{X} \times \mathcal{X} \rightarrow \mathbb{R}$
 - Number of nearest neighbors to consider: k
- **Prediction rule**
 - New example x'
 - K-nearest neighbors: k training examples with largest $K(\vec{x}_i, \vec{x}')$

$$h(\vec{x}') = \arg \max_{y \in Y} \left\{ \sum_{i \in k\text{nn}(\vec{x}')} \mathbf{1}_{\{y_i=y\}} K(\vec{x}_i, \vec{x}') \right\}$$

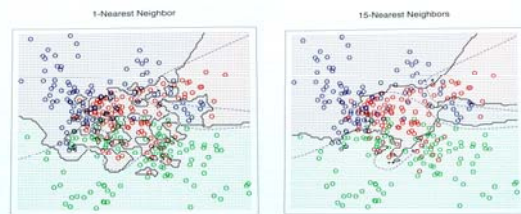
Types of Attributes

- **Symbolic (nominal)**
 - EyeColor {brown, blue, green}
- **Boolean**
 - anemic {TRUE, FALSE}
- **Numeric**
 - Integer: age [0, 105]
 - Real: length
- **Structural**
 - Natural language sentence: parse tree
 - Protein: sequence of amino acids

Example: Expensive Housing (>\$200 / sqft)



Example: Effect of k



Hastie, Tibshirani, Friedman 2001

Supervised Learning (Concept Learning, Classification, Regression, etc.)

- **Task:**
 - Learn (to imitate) a function $f: X \rightarrow Y$
- **Training Examples:**
 - Learning algorithm is given the correct value of the function for particular inputs \rightarrow **training examples**
 - An **example** is a pair $(x, f(x))$, where x is the input and $f(x)$ is the output of the function applied to x .
- **Goal:**
 - Find a function

$h: X \rightarrow Y$	that approximates
$f: X \rightarrow Y$	as well as possible.

Weighted K-Nearest Neighbor for Regression

- **Given: Training data** $(\vec{x}_1, y_1), \dots, (\vec{x}_n, y_n)$
 - Attribute vectors: $\vec{x}_i \in \mathcal{X}$
 - Target attribute: $y_i \in \mathbb{R}$
- **Parameter:**
 - Similarity function: $K : \mathcal{X} \times \mathcal{X} \rightarrow \mathbb{R}$
 - Number of nearest neighbors to consider: k
- **Prediction rule**
 - New example x'
 - K-nearest neighbors: k training examples with largest $K(\vec{x}_i, \vec{x}')$

$$h(\vec{x}') = \frac{\sum_{i \in k\text{nn}(\vec{x}')} y_i K(\vec{x}_i, \vec{x}')}{\sum_{i \in k\text{nn}(\vec{x}')} K(\vec{x}_i, \vec{x}')}$$

Collaborative Filtering

