# Light Reflection and Illumination 

## CS 4620 Lecture 35

## Shading

- Variation in observed color across an object
- strongly affected by lighting
- present even for homogeneous material
- caused by how a material reflects light
- depends on
- geometry
- lighting
- material
- therefore gives cues to all 3

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## Shading for Computer Graphics

- Need to compute an image
- of particular geometry
- under particular illumination
- from a particular viewpoint
- Basic question: how much light reflects from an object toward the viewer?


## Diffuse + Phong shading



## Mirror reflection

- Consider perfectly shiny surface
- there isn't a highlight
- instead there's a reflection of other objects
- Can render this using recursive ray tracing
- to find out mirror reflection color, ask what color is seen from surface point in reflection direction
- already computing reflection direction for Phong...
- "Glazed" material has mirror reflection and diffuse

$$
L=L_{a}+L_{d}+L_{m}
$$

- where $L_{m}$ is evaluated by tracing a new ray


## Mirror reflection

- Intensity depends on view direction
- reflects incident light from mirror direction


$$
\begin{aligned}
\mathbf{r} & =\mathbf{v}+2((\mathbf{n} \cdot \mathbf{v}) \mathbf{n}-\mathbf{v}) \\
& =2(\mathbf{n} \cdot \mathbf{v}) \mathbf{n}-\mathbf{v}
\end{aligned}
$$

## Diffuse + mirror reflection (glazed)


(glazed material on floor)

## Fancier shading

- Diffuse + Phong has long been the heuristic baseline for surface shading
- Newer/better methods are more based on physics
- when writing a shader, think like a bug standing on the surface
- bug sees an incident distribution of light that is arriving at the surface
- physics question: what is the outgoing distribution of light?


## Simple materials



## metal


dielectric

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## Adding microgeometry



## Classic reflection behavior



Lambertian

## Specular reflection

- Smooth surfaces of pure materials have ideal specular reflection (said this before)
- Metals (conductors) and dielectrics (insulators) behave differently
- Reflectance (fraction of light reflected) and angle of reflection/refraction depend on angle

dielectric


## Refraction at boundary of media



## Snell's Law

- Tells us where the refracted ray goes
- Computation
- ratio of sines is ratio of in-plane components
- project to surface; scale by eta ratio; recompute normaldirection component

$\eta_{1} \sin \theta_{1}=\eta_{2} \sin \theta_{2}$
- total internal reflection


## Computing Ray Directions



$$
s_{2}=\left(\eta_{1} / \eta_{2}\right) s_{1}
$$

## Total Internal Reflection

- Occurs when $\mathrm{s}_{2}>1$
- All light is reflected; no refraction


Photo by Brocken Inaglory

## Ray tracing dielectrics

- Like a simple mirror surface, use recursive ray tracing
- But we need two rays
- One reflects off the surface (same as mirror ray)
- The other crosses the surface (computed using Snell's law)
- Doesn't always exist (total internal reflection)
- Splitting into two rays, recursively, creates a ray tree
- Very many rays are traced per viewing ray
- Ways to prune the tree
- Limit on ray depth
- Limit on ray attenuation


## Specular reflection from metal

- Reflectance does depend on angle
- but not much
- safely ignored in basic rendering

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## Specular reflection from glass/water

- Dependence on angle is dramatic!

Glass

- about 4\% at normal incidence
- always 100\% at grazing
- remaining light is transmitted
- This is important for proper appearance

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## Fresnel reflection


constant reflectance


Fresnel reflectance

## Fresnel's formulas

- They predict how much light reflects from a smooth interface between two materials
- usually one material is empty space

$$
\begin{aligned}
F_{p} & =\frac{\eta_{2} \cos \theta_{1}-\eta_{1} \cos \theta_{2}}{\eta_{2} \cos \theta_{1}+\eta_{1} \cos \theta_{2}} \\
F_{s} & =\frac{\eta_{1} \cos \theta_{1}-\eta_{2} \cos \theta_{2}}{\eta_{1} \cos \theta_{1}+\eta_{2} \cos \theta_{2}} \\
R & =\frac{1}{2}\left(F_{p}^{2}+F_{s}^{2}\right)
\end{aligned}
$$

$-R$ is the fraction that is reflected

- $(1-R)$ is the fraction that is transmitted


## Schlick's approximation

- For graphics, a quick hack to get close with less computation:

$$
\tilde{R}=R_{0}+\left(1-R_{0}\right)(1-\cos \theta)^{5}
$$

- $R_{0}$ is easy to compute:

$$
\begin{aligned}
F_{p} & =\frac{\eta_{2}-\eta_{1}}{\eta_{2}+\eta_{1}} \\
F_{s} & =\frac{\eta_{1}-\eta_{2}}{\eta_{1}+\eta_{2}} \\
R_{0} & =\left(\frac{\eta_{2}-\eta_{1}}{\eta_{2}+\eta_{1}}\right)^{2}
\end{aligned}
$$



## Fresnel reflection



|  | diffuse | glossy | mirror |
| :--- | :--- | :--- | :--- |
| indirect | soft indirect <br> illumination | blurry <br> reflections of <br> other objects | reflected <br> images of other <br> objects |
| environment | soft shadows | blurry <br> reflection of <br> environment | reflected image <br> of environment |
| area | soft shadows | shaped specular <br> highlight | reflected image <br> of source |
| point/ <br> directional | hard shadows | simple specular <br> highlight | point <br> reflections |

$$
\square=\text { easy to include in "classic" ray tracer }
$$

## BRDF



## Reciprocity

- Interchanging arguments
- Physical requirement



## Energy Conservation

- Reflected power < incident power
- Physical requirement


