

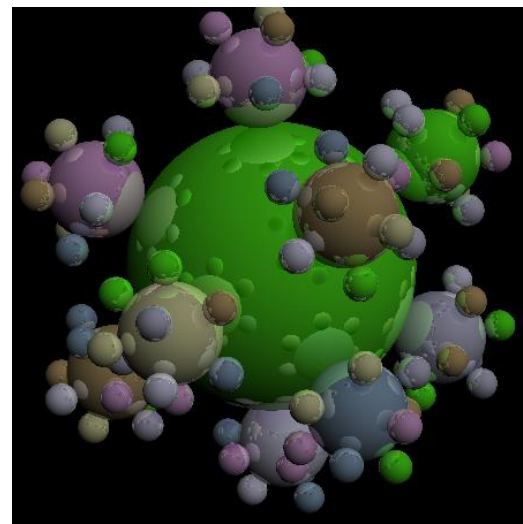
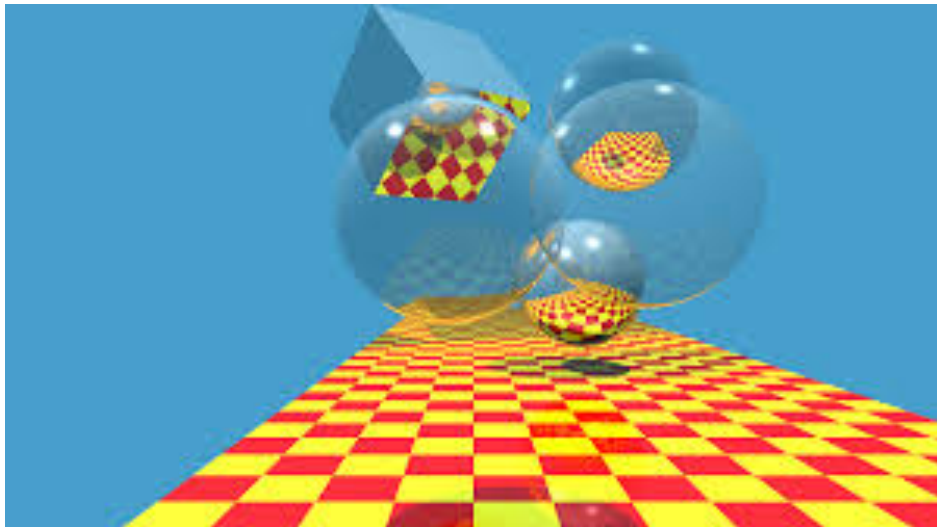
Ray Tracing

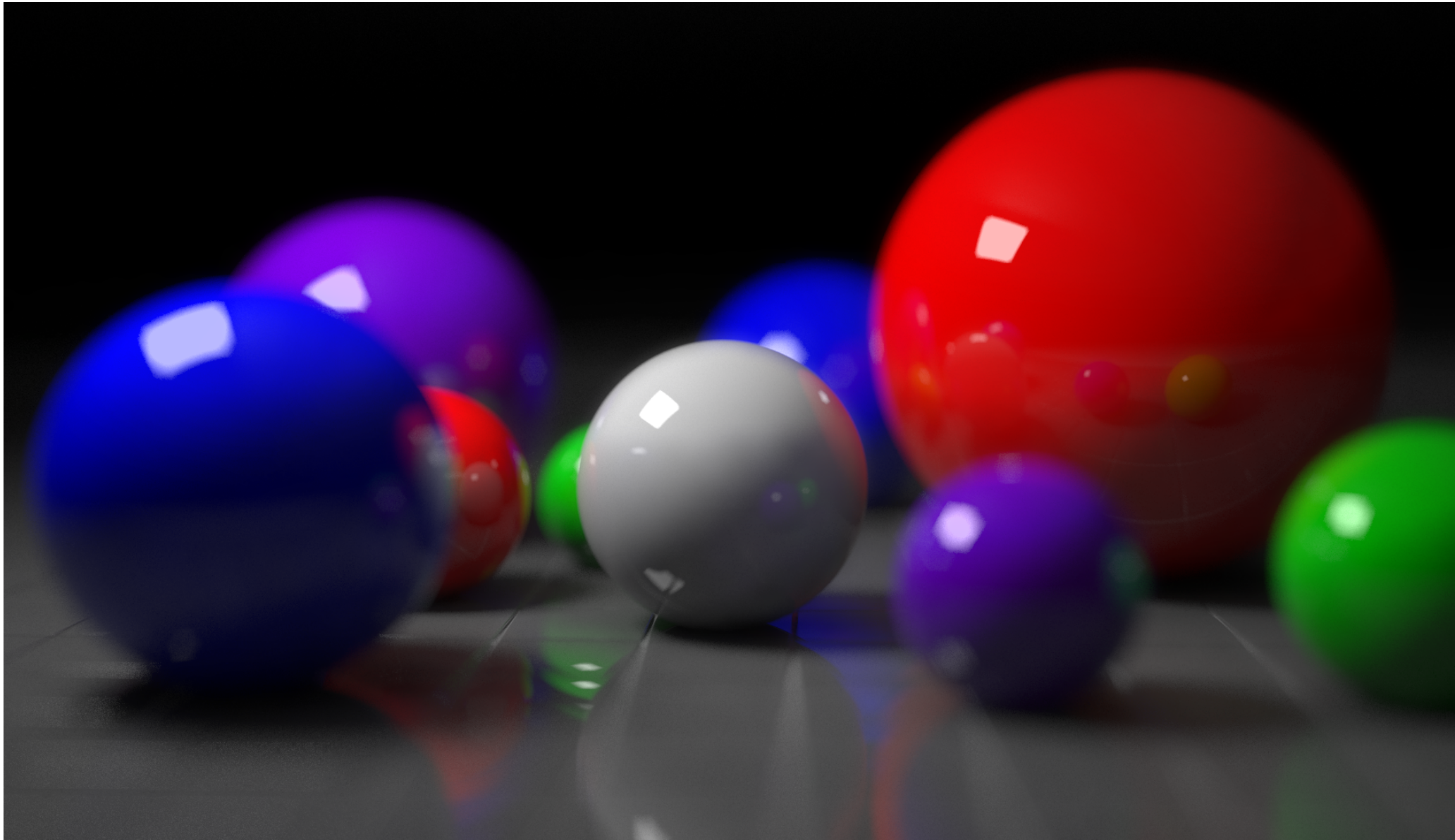
CS 4620 Lecture 34

Next few weeks

- This week
 - Ray Tracing
 - 462 I: Meet with TAs for feedback
 - A6 due
- Next week
 - Ray Tracing
 - TG!
- Last week of classes
 - Imaging, Research
 - A7 due

Back to ray tracing







Topics

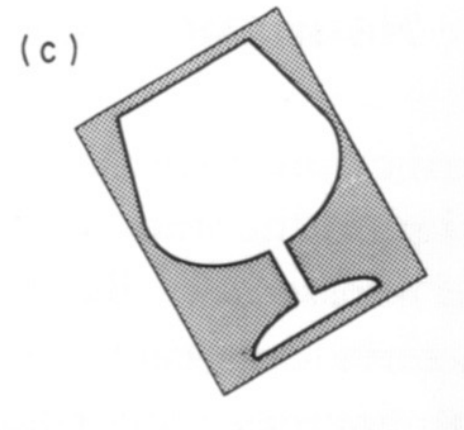
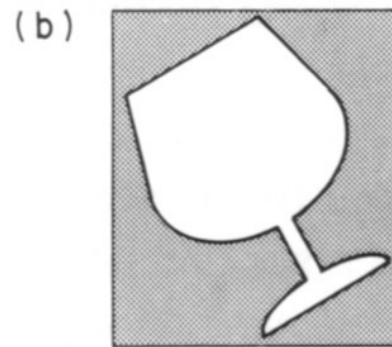
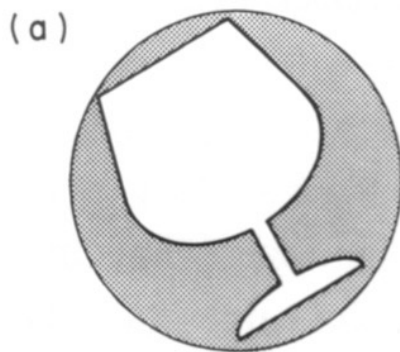
- Ray tracing acceleration structures
 - Bounding volumes
 - Bounding volume hierarchies
 - Uniform spatial subdivision
 - Adaptive spatial subdivision
- Transformations in ray tracing
 - Transforming objects
 - Transformation hierarchies

Ray tracing acceleration

- Ray tracing is slow. This is bad!
 - Ray tracers spend most of their time in ray-surface intersection methods
- Ways to improve speed
 - Make intersection methods more efficient
 - Yes, good idea. But only gets you so far
 - Call intersection methods fewer times
 - Intersecting every ray with every object is wasteful
 - Basic strategy: efficiently find big chunks of geometry that definitely do not intersect a ray

Bounding volumes

- Quick way to avoid intersections: bound object with a simple volume
 - Object is fully contained in the volume
 - If it doesn't hit the volume, it doesn't hit the object
 - So test bvol first, then test object if it hits



Bounding volumes

- Cost: more for hits and near misses, less for far misses
- Worth doing? It depends:
 - Cost of bvol intersection test should be small
 - Therefore use simple shapes (spheres, boxes, ...)
 - Cost of object intersect test should be large
 - Bvols most useful for complex objects
 - Tightness of fit should be good
 - Loose fit leads to extra object intersections
 - Tradeoff between tightness and bvol intersection cost

Implementing bounding volume

- Just add new Surface subclass, “BoundedSurface”
 - Contains a bounding volume and a reference to a surface
 - Intersection method:
 - Intersect with bvol, return false for miss
 - Return `surface.intersect(ray)`
 - This change is transparent to the renderer (only it might run faster)
- Note that all Surfaces will need to be able to supply bounding volumes for themselves

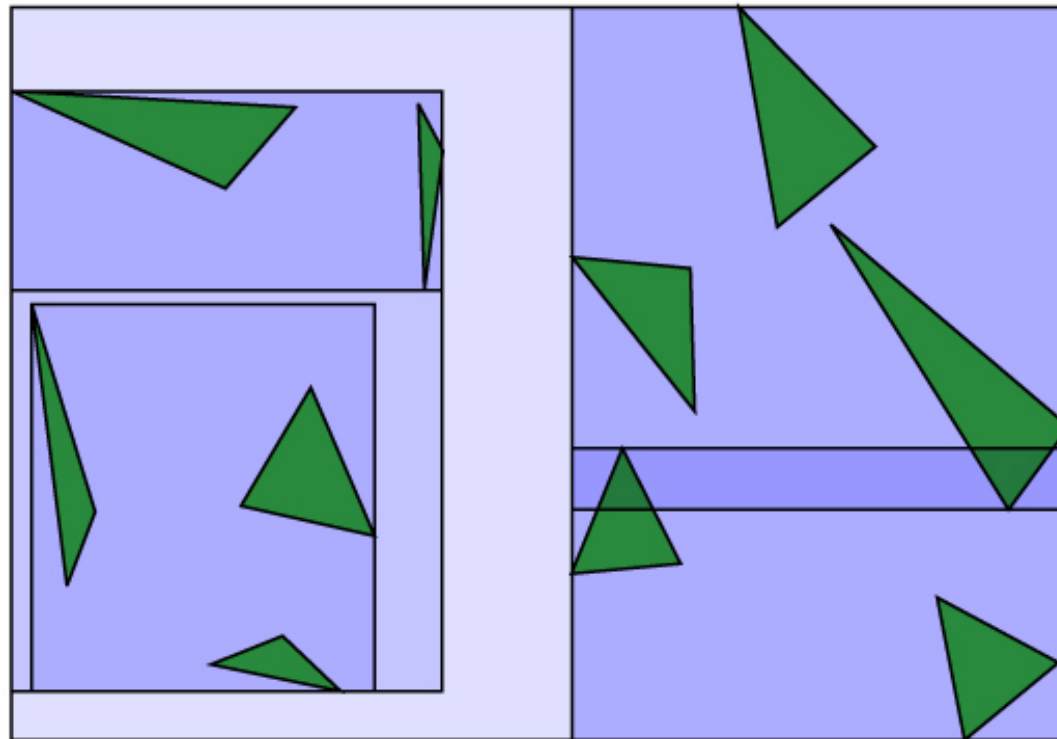
If it's worth doing, it's worth doing hierarchically!

- Bvols around objects may help
- Bvols around groups of objects will help
- Bvols around parts of complex objects will help
- Leads to the idea of using bounding volumes all the way from the whole scene down to groups of a few objects

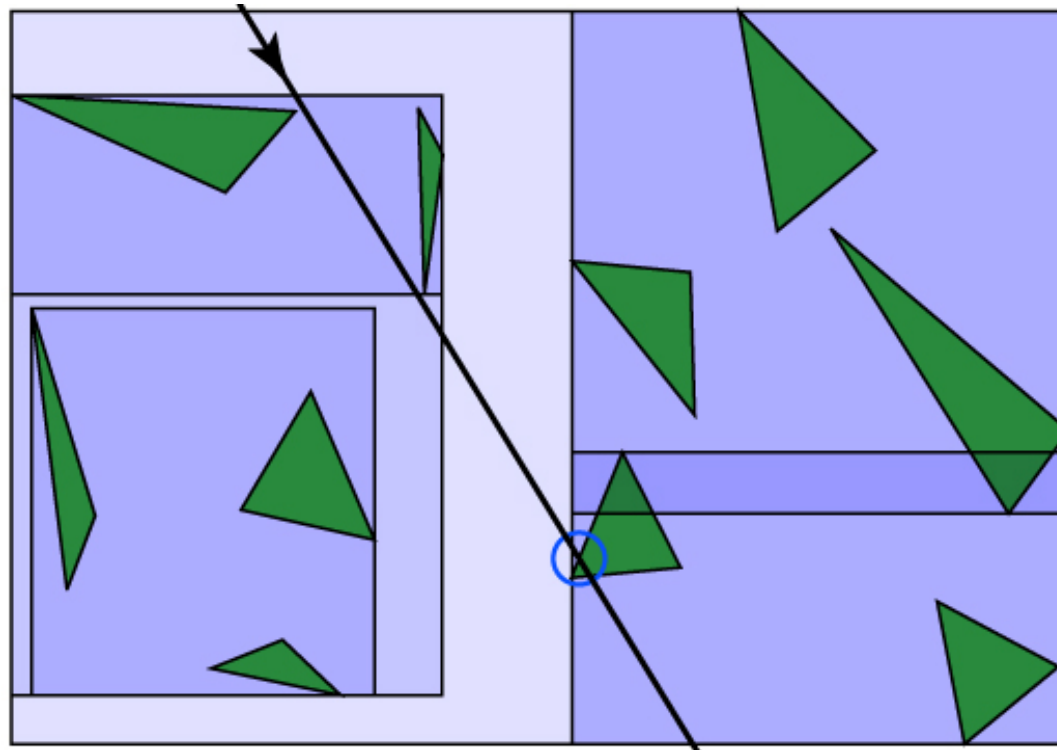
Implementing a bvol hierarchy

- A BoundedSurface can contain a list of Surfaces
- Some of those Surfaces might be more BoundedSurfaces
- Voilà! A bounding volume hierarchy
 - And it's all still transparent to the renderer

BVH construction example



BVH ray-tracing example



BVH Intersection

- Trace ray with root node
- If intersection, trace rays with ALL children
 - If no intersection, eliminate tests with all children

Choice of bounding volumes

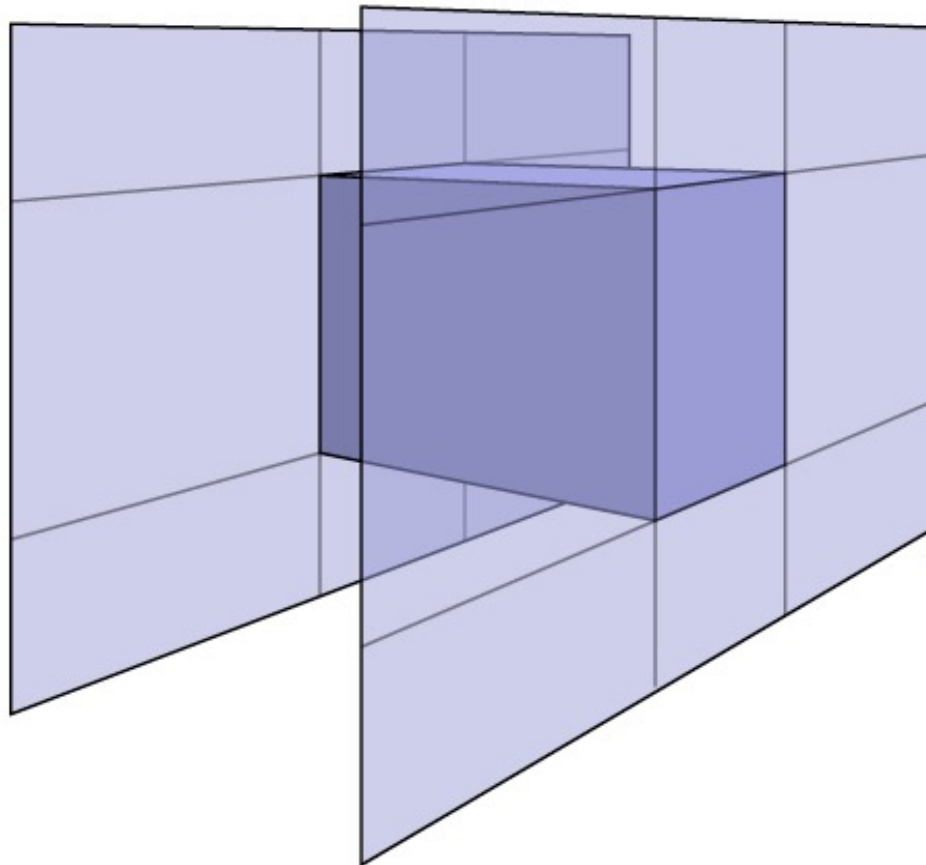
- Spheres -- easy to intersect, not always so tight
- Axis-aligned bounding boxes (AABBs) -- easy to intersect, often tighter (esp. for axis-aligned models)
- Oriented bounding boxes (OBBs) -- easy to intersect (but cost of transformation), tighter for arbitrary objects
- Computing the bvols
 - For primitives -- generally pretty easy
 - For groups -- not so easy for OBBs (to do well)
 - For transformed surfaces -- not so easy for spheres

Axis aligned bounding boxes

- Probably easiest to implement
- Computing for primitives
 - Cube: duh!
 - Sphere, cylinder, etc.: pretty obvious
 - Groups or meshes: min/max of component parts
- AABBs for transformed surface
 - Easy to do conservatively: bbox of the 8 corners of the bbox of the untransformed surface
- How to intersect them
 - Treat them as an intersection of slabs (see Shirley)

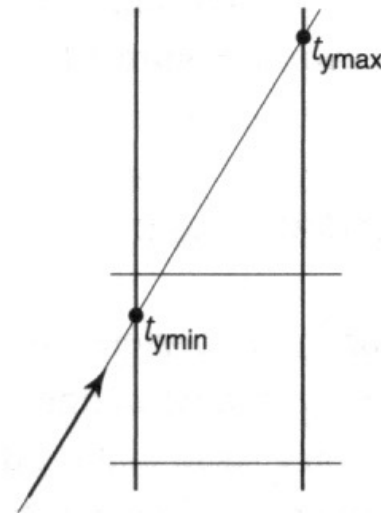
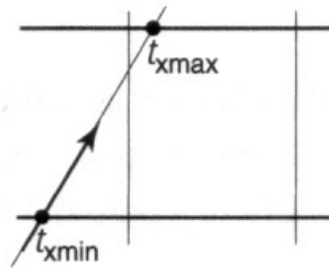
Ray-box intersection

- Could intersect with 6 faces individually
- Better way: box is the intersection of 3 slabs



Intersecting boxes: 2D

- 2D example
- 3D is the same!



$$t \in [t_{xmin}, t_{xmax}]$$

$$t \in [t_{ymin}, t_{ymax}]$$

$$t \in [t_{xmin}, t_{xmax}] \cap [t_{ymin}, t_{ymax}]$$

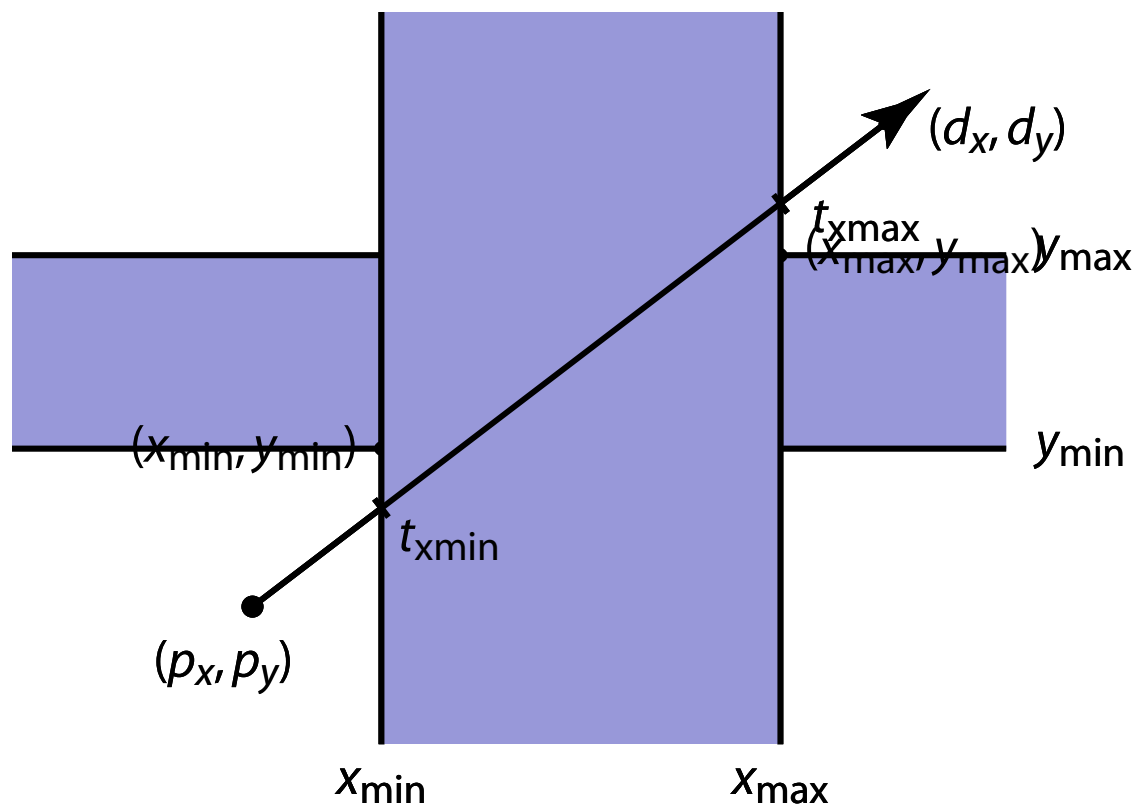
Ray-slab intersection

$$p_x + t_{x\min} d_x = x_{\min}$$

$$t_{x\min} = (x_{\min} - p_x) / d_x$$

$$p_y + t_{y\min} d_y = y_{\min}$$

$$t_{y\min} = (y_{\min} - p_y) / d_y$$



Intersecting intersections

- Each intersection is an interval
- Want last entry point and first exit point

$$t_{xenter} = \min(t_{xmin}, t_{xmax})$$

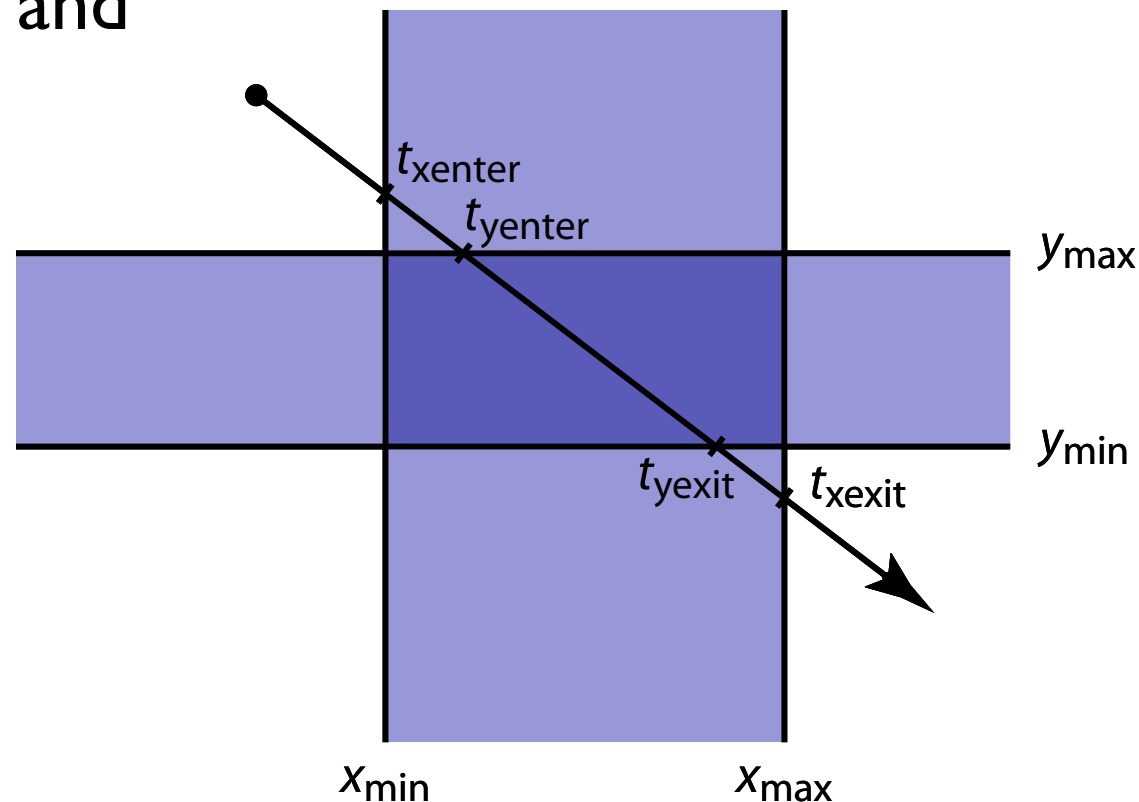
$$t_{xexit} = \max(t_{xmin}, t_{xmax})$$

$$t_{yenter} = \min(t_{ymin}, t_{ymax})$$

$$t_{yexit} = \max(t_{ymin}, t_{ymax})$$

$$t_{enter} = \max(t_{xenter}, t_{yenter})$$

$$t_{exit} = \min(t_{xexit}, t_{yexit})$$



Building a hierarchy

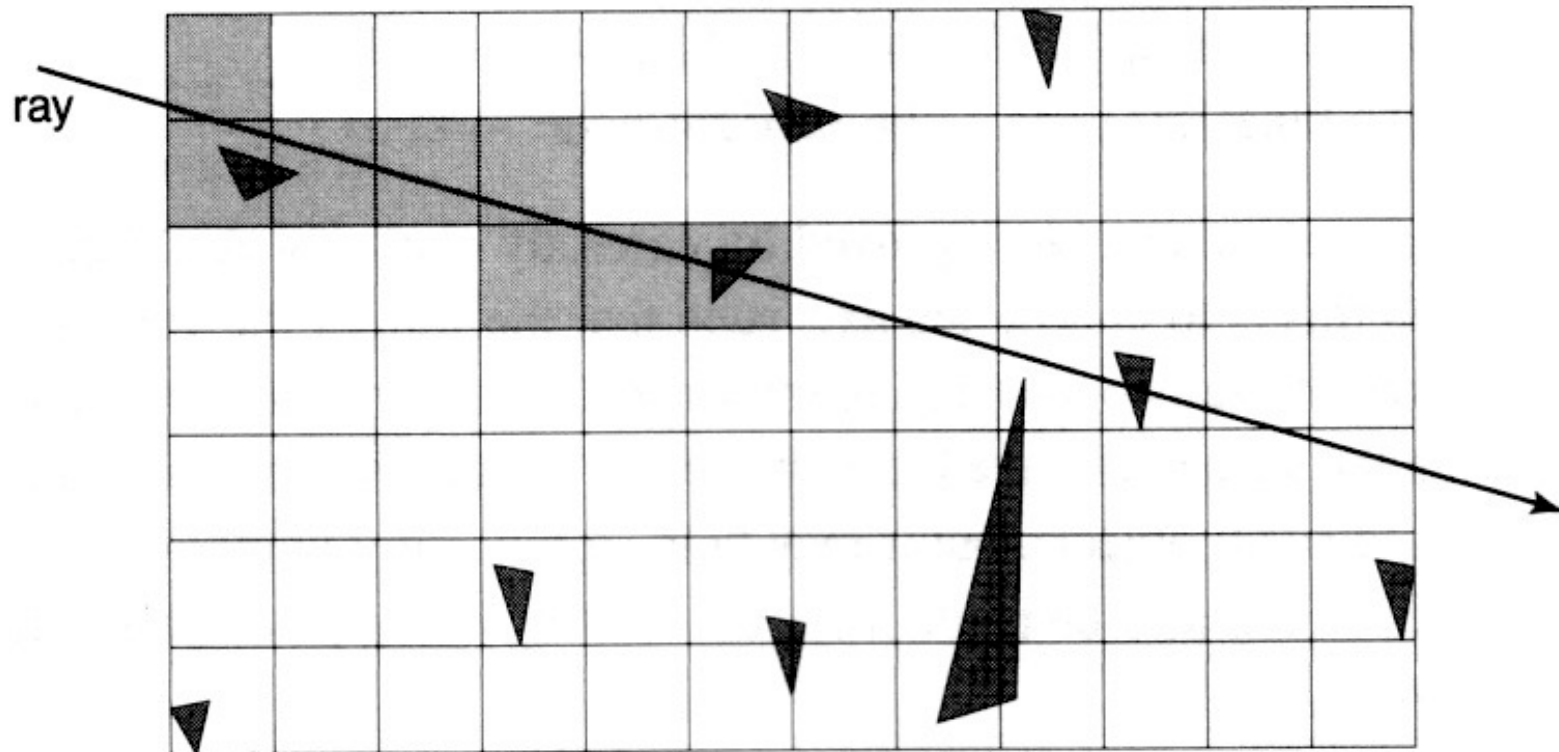
- Top Down vs Bottom Up
- Top down
 - Make bbox for whole scene, then split into (maybe 2) parts
 - Recurse on parts
 - Stop when there are just a few objects in your box
- Bottom Up
 - Ideal: partitions
 - Expensive, but optimal
 - Good for static (maybe)

Building a hierarchy

- How to partition?
 - Ideal: clusters
 - Practical: partition along axis
 - Center partition
 - Less expensive, simpler
 - Unbalanced tree
 - Median partition
 - More expensive
 - More balanced tree
 - Surface area heuristic
 - Model expected cost of ray intersection
 - Generally produces best-performing trees

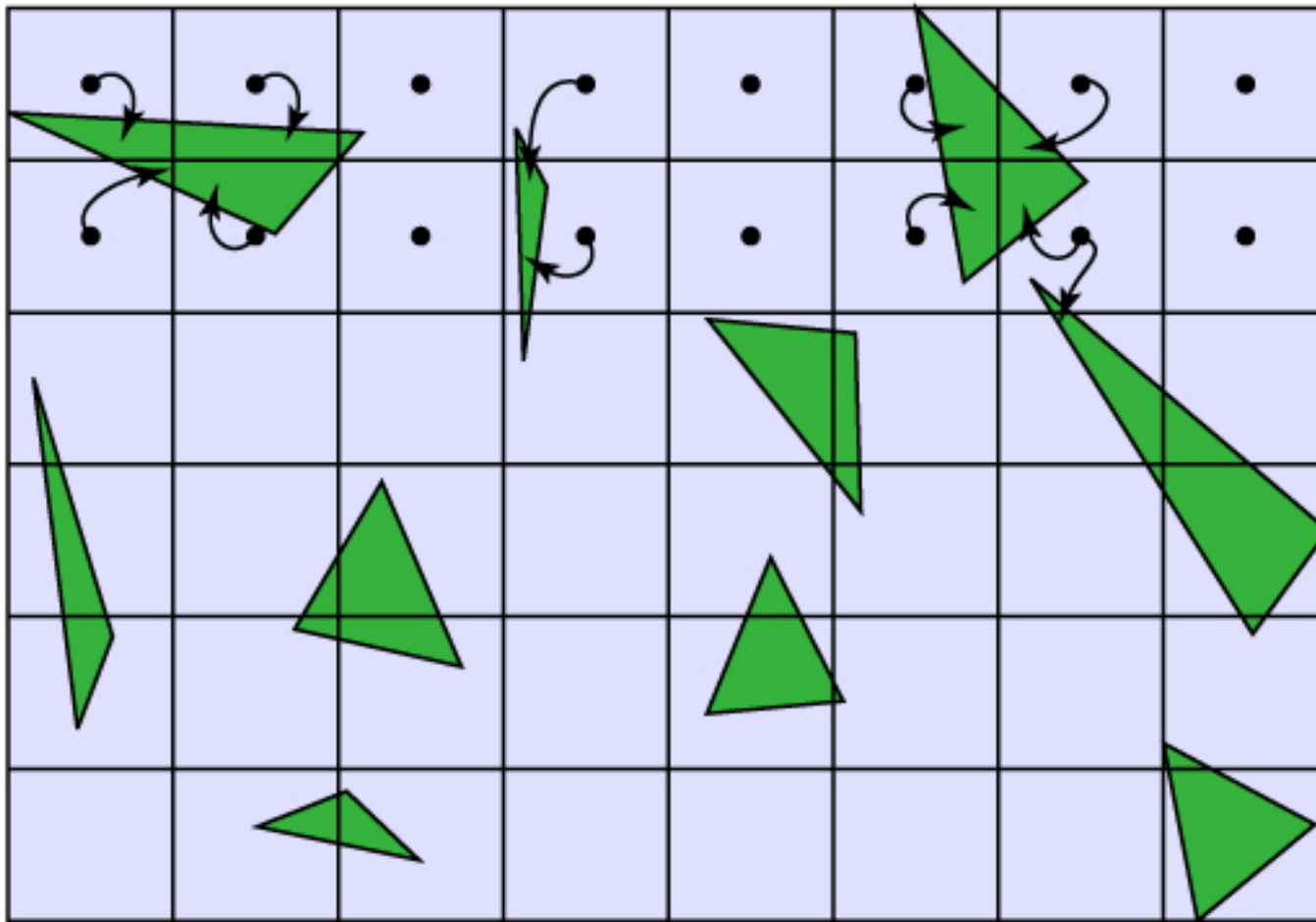
Regular space subdivision

- An entirely different approach: uniform grid of cells

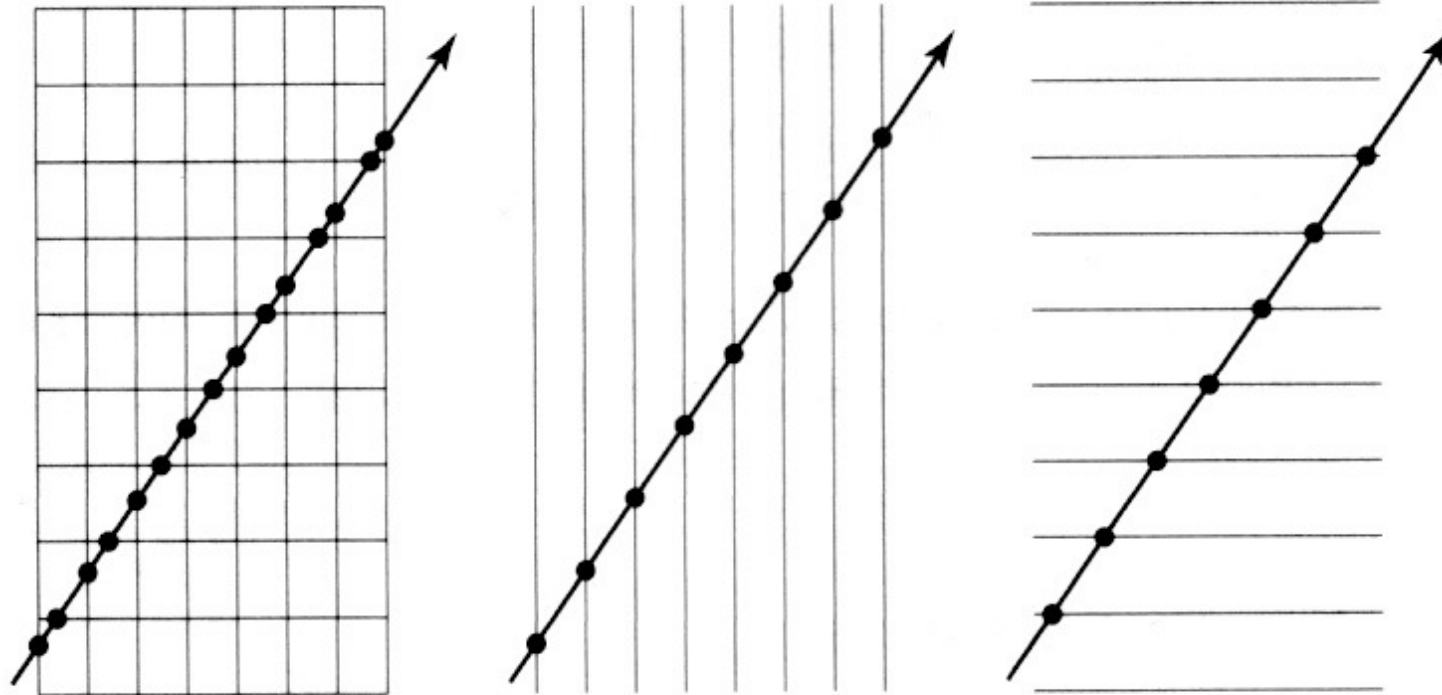


Regular grid example

- Grid divides space, not objects

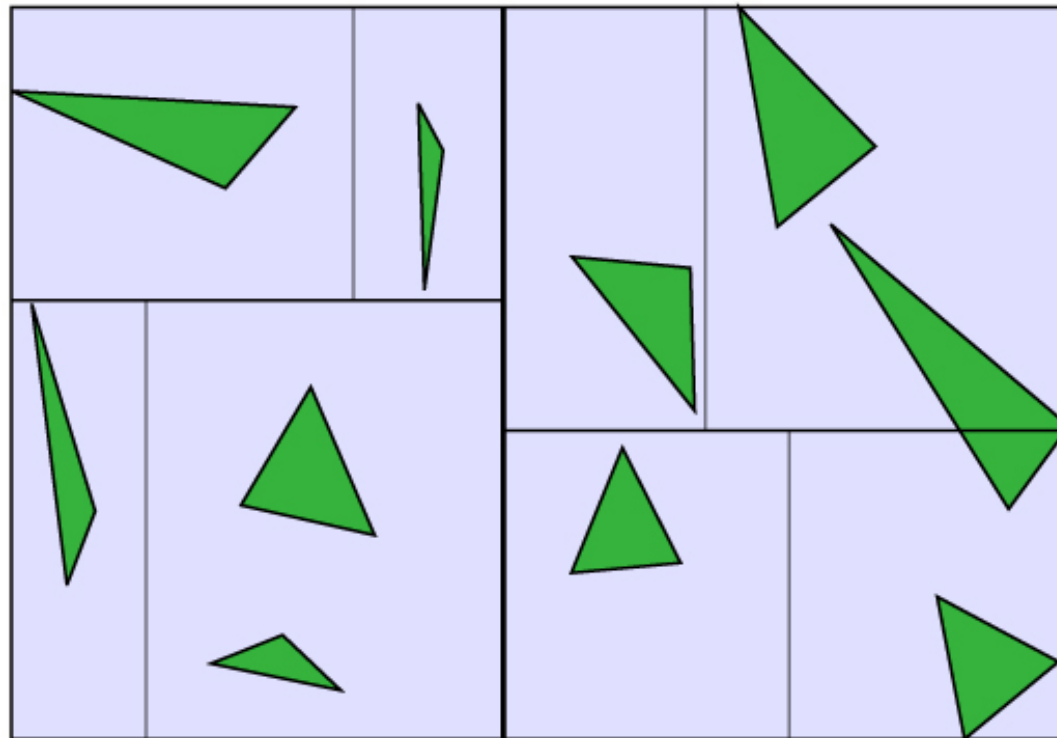


Traversing a regular grid



Non-regular space subdivision

- *k*-d Tree
 - subdivides space, like grid
 - adaptive, like BVH



Implementing acceleration structures

- Conceptually simple to build acceleration structure into scene structure
- Better engineering decision to separate them