#### CS412/CS413

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#### Lecture 30: Loop Optimizations and Pointer Analysis 07 Apr 08

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# Loop optimizations

- Now we know which are the loops
- Next: optimize these loops
  - Loop invariant code motion [last time]
  - Strength reduction of induction variables
  - Induction variable elimination

#### **Induction Variables**

- An induction variable is a variable in a loop, whose value is a function of the loop iteration number v = f(i)
- In compilers, this a linear function:

 $f(i) = c^*i + d$ 

- Observation: linear combinations of linear functions are linear functions
  - Consequence: linear combinations of induction variables are induction variables

#### Families of Induction Variables

• Basic induction variable: a variable whose only definition in the loop body is of the form

i = i + C

where c is a loop-invariant value

- Derived induction variables: Each basic induction variable i defines a family of induction variables Family(i)
  - $i \in Family(i)$
  - $k \in Family(i)$  if there is only one definition of k in the loop body , and it has the form  $k = c^*j$  or k=j+c, where
    - (a)  $j \in Family(i)$
    - (b) c is loop invariant
    - (c) The only definition of j that reaches the definition of k is in the loop
    - (d) There is no definition of i between the definitions of j and k

#### Representation

- Representation of induction variables in family i by triples:
  - Denote basic induction variable i by <i, 1, 0>
  - Denote induction variable k=i\*a+b by triple <i, a, b>

# **Finding Induction Variables**

Scan loop body to find all basic induction variables

#### do

Scan loop to find all variables k with one assignment of form k = j\*b, where j is an induction variable <i,c,d>, and make k an induction variable with triple <i,c\*b,d>

Scan loop to find all variables k with one assignment of form k = j±b where j is an induction variable with triple <i,c,d>, and make k an induction variable with triple <i,c,b±d>

until no more induction variables found

# **Strength Reduction**

 Basic idea: replace expensive operations (multiplications) with cheaper ones (additions) in definitions of induction variables

Benefit: cheaper to compute s = s+6 than j = 3\*i

$$-s = s+6$$
 requires an addition

 $- j = 3^*i$  requires a multiplication

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# **General Algorithm**

• Algorithm:

For each induction variable j with triple <i,a,b> whose definition involves multiplication:

- 1. create a new variable s
- 2. replace definition of j with j=s
- 3. immediately after i=i+c, insert s = s+a\*c
   (here a\*c is constant)
- 4. insert  $s = a^{*}i + b$  into preheader
- Correctness: transformation maintains invariant s = a\*i+b

## **Strength Reduction**

 Gives opportunities for copy propagation, dead code elimination



#### Induction Variable Elimination

- Idea: eliminate each basic induction variable whose only uses are in loop test conditions and in their own definitions i = i+c
  - rewrite loop test to eliminate induction variable

```
s = 3*i+1;
while (i<10) {
    a[s] = a[s] -2;
    i = i+2;
    s= s+6;
}
```

- When are induction variables used only in loop tests?
  - Usually, after strength reduction
  - Use algorithm from strength reduction even if definitions of induction variables don't involve multiplications

#### Induction Variable Elimination

- Rewrite test condition using derived induction variables
- Remove definition of basic induction variables (if not used after the loop)

$$s = 3^{*}i+1; \\ s = 3^{*}i+1; \\ while (i<10) \{ \\ a[s] = a[s] -2; \\ i = i+2; \\ s = s+6; \\ \}$$

#### Induction Variable Elimination

For each basic induction variable i whose only uses are

- The test condition i < u</li>
- The definition of i: i = i + c
  - Take a derived induction variable k in family i, with triple <i,c,d>
  - Replace test condition i < u with  $k < c^*u+d$
  - Remove definition i = i+c if i is not live on loop exit

#### Where We Are

- Defined dataflow analysis framework
- Used it for several analyses
  - Live variables
  - Available expressions
  - Reaching definitions
  - Constant folding
- Loop transformations
  - Loop invariant code motion
  - Induction variables
- Next:
  - Pointer alias analysis

#### **Pointer Alias Analysis**

- Most languages use variables containing addresses
  - E.g. pointers (C,C++), references (Java), call-byreference parameters (Pascal, C++, Fortran)
- Pointer aliases: multiple names for the same memory location, which occur when dereferencing variables that hold memory addresses
- Problem:
  - Don't know what variables read and written by accesses via pointer aliases (e.g. \*p=y; x=\*p; p->f=y; x=p->f; etc.)
  - Need to know accessed variables to compute dataflow information after each instruction

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## **Pointer Alias Analysis**

- Worst case scenarios
  - \*p = y may write any memory location
  - x = \*p may read any memory location
- Such assumptions may affect the precision of other analyses
- Example1: Live variables
   before any instruction x = \*p, all the variables may be live
- Example 2: Constant folding

   a = 1; b = 2;\*p = 0; c = a+b;
- c = 3 at the end of code only if \*p is not an alias for a or b!
- Conclusion: precision of result for all other analyses depends on the amount of alias information available
  - hence, it is a fundamental analysis

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#### Alias Analysis Problem

- Goal: for each variable v that may hold an address, compute the set Ptr(v) of possible targets of v
  - Ptr(v) is a set of variables (or objects)
  - Ptr(v) includes stack- and heap-allocated variables (objects)
- Is a "may" analysis: if x ∈ Ptr(v), then v may hold the address of x in some execution of the program
- No alias information: for each variable v, Ptr(v) = V, where V is the set of all variables in the program

# Simple Alias Analyses

- Address-taken analysis:
  - Consider AT = set of variables whose addresses are taken
  - Then, Ptr(v) = AT, for each pointer variable v
  - Addresses of heap variables are always taken at allocation sites (e.g., x = new int[2]; x=malloc(8); )
  - Hence AT includes all heap variables
- Type-based alias analysis:
  - If v is a pointer (or reference) to type T, then Ptr(v) is the set of all variables of type T
  - Example: p->f and q->f can be aliases only if p and q are references to objects of the same type
  - Works only for strongly-typed languages

#### **Dataflow Alias Analysis**

- Dataflow analysis: for each variable v, compute pointsto set Ptr(v) at each program point
- Dataflow information: set Ptr(v) for each variable v
  - Can be represented as a graph G  $\subseteq$  2 <sup>V × V</sup>
  - Nodes = V (program variables)
  - There is an edge  $v \rightarrow u$  if  $u \in Ptr(v)$



#### **Dataflow Alias Analysis**

• Dataflow Lattice:  $(2 \vee \times \vee, \supseteq)$ 

- V x V represents "every variable may point to every var."

- "may" analysis: top element is  $\emptyset$ , meet operation is  $\cup$
- Transfer functions: use standard dataflow transfer functions: out[I] = (in[I]-kill[I]) U gen[I]
  - $p = addr q \qquad kill[1] = \{p\} \times V \qquad gen[1] = \{<p,q>\} \\ p = q \qquad kill[1] = \{p\} \times V \qquad gen[1] = \{p\} \times Ptr(q) \\ p = *q \qquad kill[1] = \{p\} \times V \qquad gen[1] = \{p\} \times Ptr(Ptr(q)) \\ *p = q \qquad kill[1] = ... \qquad gen[1] = Ptr(p) \times Ptr(q) \\ For all other instruction, kill[1] = \{\}, gen[1] = \{\}$
- Transfer functions are monotonic, but not distributive!

#### Alias Analysis Example



# Alias Analysis Uses

- Once alias information is available, use it in other dataflow analyses
- Example: Live variable analysis
   Use alias information to compute use[I] and def[I] for load and store statements:

$$x = *y$$
use[I] = {y} U Ptr(y)def[I]={x} $*x = y$ use[I] = {x,y}def[I]=Ptr(x)