CS412/413

Introduction to Compilers Tim Teitelbaum

Lecture 29: Control Flow Analysis and Loop Optimization 4 Apr 08

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Introduction to Compilers

Agenda

- Discovering loops in control-flow graphs
 - Dominators
 - Compute dominators by data-flow analysis
- Loop invariant code motion
 - Discovering loop-invariant definitions
 - Application of reaching definitions
 - Validating movement of loop-invariant definition
 - Application of live variable analysis
 - Application of reaching definitions

Program Loops

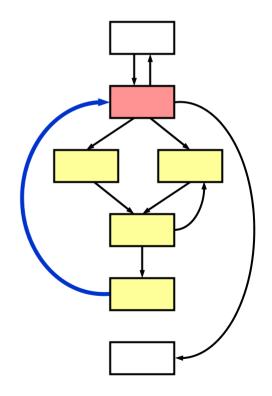
- Loop = a computation repeatedly executed until a terminating condition is reached
- High-level loop constructs:
 - While loop: while(E) S
 - Do-while loop: do S while(E)
 - For loop: for(i=1; i<=u; i+=c) S</pre>
- Why are loops important:
 - Most of the execution time is spent in loops
 - Typically: 90/10 rule, 10% code is a loop
- Therefore, loops are important targets of optimizations

Detecting Loops

- Need to identify loops in the program
 - Easy to detect loops in high-level constructs
 - Harder to detect loops in low-level code or in general control-flow graphs
- Examples where loop detection is difficult:
 - Languages with unstructured "goto" constructs: structure of high-level loop constructs may be destroyed
 - Optimizing Java bytecodes (without high-level source program): only low-level code is available

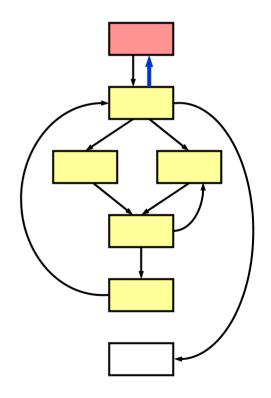
Control-Flow Analysis

- Goal: identify loops in the control flow graph
- A loop in the CFG:
 - Is a set of CFG nodes (basic blocks)
 - Has a loop header such that control to all nodes in the loop always goes through the header
 - Has a back edge from one of its nodes to the header



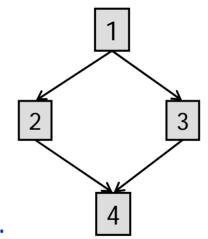
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Dominators

- Use concept of dominators in CFG to identify loops
- Node d dominates node n if all paths from the entry node to n go through d



Every node dominates itself 1 dominates 1, 2, 3, 4 2 doesn't dominate 4 3 doesn't dominate 4

- Intuition:
 - Header of a loop dominates all nodes in loop body
 - Back edges = edges whose heads dominate their tails
 - Loop identification = back edge identification

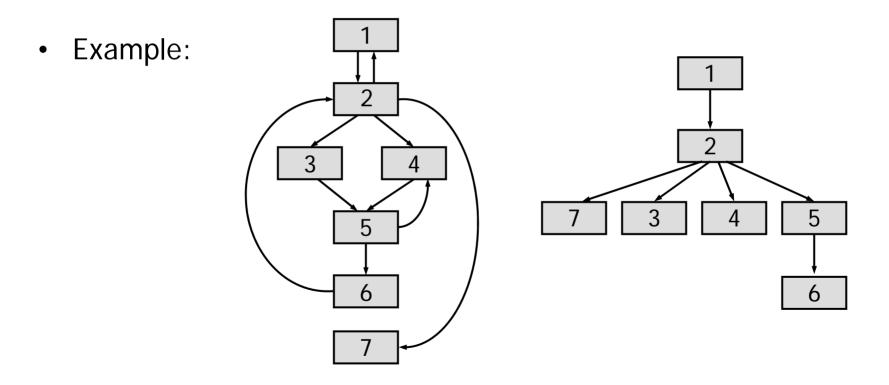
Immediate Dominators

• Properties:

- 1. CFG entry node n₀ dominates all CFG nodes
- 2. If d1 and d2 dominate n, then either
- d1 dominates d2, or
- d2 dominates d1
- d strictly dominates n if d dominates n and $d\neq n$
- The immediate dominator idom(n) of a node n is the unique last strict dominator on any path from n₀ to n

Dominator Tree

- Build a dominator tree as follows:
 - Root is CFG entry node n₀
 - m is child of node n iff n=idom(m)

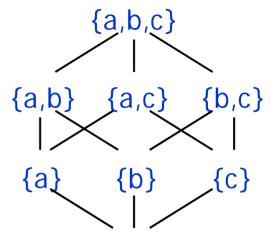


Computing Dominators

- Formulate problem as a system of constraints:
 - Define dom(n) = set of nodes that dominate n
 - $\text{ dom}(n_0) = \{n_0\}$
 - $\text{ dom}(n) = \cap \{ \text{ dom}(m) \mid m \in \text{pred}(n) \} \cup \{n\}$
 - i.e, the dominators of n are the dominators of all of n's predecessors and n itself

Dominators as a Dataflow Problem

- Let N = set of all basic blocks
- Lattice: (2^N, ⊆); has finite height
- Meet is set intersection, top element is N
- Is a forward dataflow analysis
- Dataflow equations: out[B] = F_B(in[B]), for all B in[B] = ∩{out[B'] | B'∈pred(B)}, for all B in[B_s] = {}



 $\langle \rangle$

- Transfer functions: F_B(X) = X U {B}
 - are monotonic and distributive
- Iterative solving of dataflow equation:
 - terminates
 - computes MOP solution

Natural Loops

- Back edge: edge $n \rightarrow h$ such that h dominates n
- Natural loop of a back edge $n \rightarrow h$:
 - h is loop header
 - Set of loop nodes is set of all nodes that can reach n without going through h
- Algorithm to identify natural loops in CFG:
 - Compute dominator relation
 - Identify back edges
 - Compute the loop for each back edge

for each node h in dominator tree

for each node n for which there exists a back edge $n \rightarrow h$ define the loop with

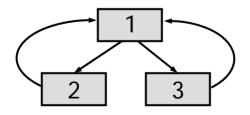
header h back edge n→h body consisting of all nodes reachable from n by a depth first search backwards from n that stops at h

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Disjoint and Nested Loops

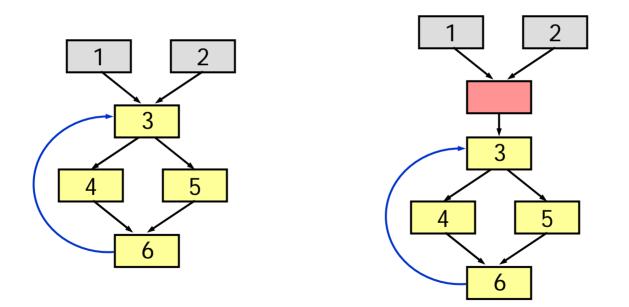
- Property: for any two natural loops in the flow graph, one of the following is true:
 - 1. They are disjoint
 - 2. They are nested
 - 3. They have the same header
- Eliminate alternative 3: if two loops have the same header and none is nested in the other, combine all nodes into a single loop



Two loops: {1,2} and {1,3} Combine into one loop: {1,2,3}

Loop Preheader

- Several optimizations add code before header
- Insert a new basic block (called preheader) in the CFG to hold this code



Loop optimizations

- Now we know the loops
- Next: optimize these loops
 - Loop invariant code motion
 - Strength reduction of induction variables
 - Induction variable elimination

Loop Invariant Code Motion

- Idea: if a computation produces same result in all loop iterations, move it out of the loop
- Example: for (i=0; i<10; i++) buf[i] = 10*i + x*x;
- Expression x*x produces the same result in each iteration; move it out of the loop:

```
t = x*x;
for (i=0; i<10; i++)
buf[i] = 10*i + t;
```

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Loop Invariant Computation

- An instruction a = b OP c is loop-invariant if each operand is:
 - Constant, or
 - Has all definitions outside the loop, or
 - Has exactly one definition, and that is a loop-invariant computation
- Reaching definitions analysis computes all the definitions of x and y that may reach t = x OP y

Algorithm

 $INV = \emptyset$ repeat **for** each instruction I in loop such that $I \notin INV$ if operands are constants, or operands have definitions outside the loop, or operands have exactly one definition $d \in INV$ then $INV = INV \cup \{I\}$ until no changes in INV

Code Motion

- Next: move loop-invariant code out of the loop
- Suppose a = b OP c is loop-invariant
- We want to hoist it out of the loop

Valid Code Motion

- Code motion of a definition d: a = b OP c to pre-header is valid if:
- 1. Definition d dominates all loop exits where a is live
 - Use dominator tree to check whether each loop exit is dominated by d
- 2. There is no other definition of a in loop
 - Scan all body for any other definitions of a
- 3. All uses of a in loop can only be reached from definition d
 - Consult reaching definitions at each use of a for any definitions of a other than d

Valid Code Motion

• Invalid example 1: $a = x^*x$; does not dominate break to use of a

• Invalid example 2: there is another definition of a in loop

for (i=0; i<10; i++)
if (f(i)) a = x*x;
else a = 0;</pre>

• Invalid example 3: use of a in loop can be reached from a=0;

a = 0; for (i=0; i<10; i++) if (f(i)) a = x*x; else buf[i] = a;

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Other Issues

- Preserve dependencies between loop-invariant instructions when hoisting code out of the loop
 - for (i=0; i<N; i++) { X = Y + Z; $t = x^{*}x$ X = Y + Z;a[i] = 10*i + x*x;for(i=0; i<N; i++) a[i] = 10*i + t;
- Nested loops: apply loop-invariant code motion algorithm multiple times

for (i=0; i<N; i++)for (j=0; j<M; j++) $a[i][j] = x^*x + 10^*i + 100^*j;$ for (j=0; j<M; j++)

 $t1 = x^*x;$ for (i=0; i<N; i++) { $t_2 = t_1 + 10^{*}i_1$ $a[i][j] = t2 + 100^{*}j;$

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