CS381
Fall 2002

Monday Oct 7, 2002
Olin 155 9:05-9;55

This is a 50 minute in class closed book exam. All questions are straight forward and you should have no trouble doing them. Please show all work and write legibly. Thank you.

1. Write a regular expression for the set of all strings of 0 's and 1 's such that the number of occurrences of the substring 01 is even. Zero occurrences is even.

Argue in English that your regular expression is correct.
2. Let $R_{i j}^{k}$ be the regular expression denoting all strings that take a finite automaton from state i to state j without going through any state numbered higher than k .
(a) Give the formula for $R_{i j}^{k}$ in terms of $R_{i j}^{l}$ for $\mathrm{l}<\mathrm{k}$.

(b) What is the regular expression for $R_{34}^{2}$ for the above state diagram?
(c) What is the regular expression for $R_{43}^{2}$ for the above state diagram?

You do not need to use the formula in (a) to get your answer to parts (b) and (c).

## Over

3. Let $M=\left(Q, \Sigma, \delta, q_{0}, F\right)$ be a deterministic finite automata. Let $\mathrm{K}=\left\{x \mid x \in \Sigma^{*}\right.$ and $\left.\exists y \in L(M),|y|=|x|\right\}$.
(a) Describe in English the set K.
(b) Construct a nondeterministic finite automaton $M_{2}=\left(Q_{2}, \Sigma, \delta_{2}, q_{02}, F_{2}\right)$ accepting the set K.
4.Let R be a regular set over the alphabet $\Sigma=\{a, b\}$. For each string in R replace the first occurrence of the substring baa by ba. Let $\hat{R}$ be the resulting set of strings. Show by using homomorphisms, inverse homomorphisms and intersection with regular sets that $\hat{R}$ is regular.
