

Read: pp. 403-408 CS1110 30 September. Recursion but SKIP sect. 15.1.2

ProgramLive CD, page 15-3, has interesting recursive methods. Download presented algorithms from the website

Prelim I
7:30-9:00PM
Thursday, 7 Oct

Recursive definition: A definition that is defined in terms of itself.
Recursive method: a method that calls itself (directly or indirectly).
Recursion is often a good alternative to iteration (loops), which we cover later. Recursion is an important programming tool. Purely functional languages have no loops —only recursion.

Recursion: If you get the point, stop; otherwise, see Recursion.
Infinite recursion: See Infinite recursion.

1

```
/** = the number of 'e's in s */
public static int noe(String s) {
    if (s.length() == 0) {
        return 0;
    }
    // { s has at least one char }
    return (s[0] == 'e' ? 1 : 0) + noe(s.substring(1));
}
```

Express the answer with the same terminology as the specification, but on a smaller scale:
number of 'e's in s = (if s[0] = 'e' then 1 else 0) + number of 'e's in s[1..]

Notation:
s[i] shorthand for s.charAt[i].
s[i..] shorthand for s.substring(i).

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Two issues in coming to grips with recursion

1. How are recursive calls executed?
2. How do we understand a recursive method and how do we create one?

We discussed the first issue earlier. If you execute a call on a recursive method carefully, using our model of execution, you will see that it works. Briefly, a new frame is created for each recursive call. We do this in the next lecture.

DON'T try to understand a recursive method by executing its recursive calls! Use execution only to understand how it works.

3

Understanding a recursive method

Step 1: HAVE A PRECISE SPECIFICATION

```
// = number of 'e's in s
public static int noe(String s) {
    if (s.length() == 0) {
        return 0;
    }
    // {s has at least one character}
    // return (s[0] == 'e' ? 1 : 0) + number of 'e's in s[1..];
    return (s[0] == 'e' ? 1 : 0) + noe(s.substring(1));
}
```

Step 2: Check the base case. When s is the empty string, 0 is returned. So the base case is handled correctly.

Notation:
s[i] shorthand for s.charAt[i].
s[i..] shorthand for s.substring(i).

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Understanding a recursive function

s = ""
s has at least one character

Step 3: Recursive calls make progress toward termination.

```
// = number of 'e's in s
public static int noe(String s) {
    if (s.length() == 0) {
        return 0;
    }
    // {s has at least one character}
    return (s[0] == 'e' ? 1 : 0) + noe(s.substring(1));
}
```

Step 4: Recursive case is correct.

argument s[1..] is smaller than parameter s, so there is progress toward reaching base case 0

parameter s
argument s[1..]

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Creating a recursive method

Task: Write a method that removes blanks from a String.

0. Specification:

```
/** = s but with its blanks removed */
public static String deblank(String s)
```

1. Base case: the smallest String s is "".

```
if (s.length() == 0)
    return s;
```

2. Other cases: String s has at least 1 character.

```
return (s[0] == ' ' ? "" : s) + s[1..] with its blanks removed
```

precise spec!
Notation:
s[i] shorthand for s.charAt[i].
s[i..] shorthand for s.substring(i).

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```
// = s but with its blanks removed
public static String deblank(String s) {
    if (s.length() == 0) return s;
    // {s is not empty}
    if (s[0] is a blank)
        return s[1..] with its blanks removed
    // {s is not empty and s[0] is not a blank}
    return s[0] + (s[1..] with its blanks removed);
}
```

The tasks given by the two English, blue expressions are similar to the task fulfilled by this function, but on a smaller String! Rewrite each as

```
deblank(s[1..]) .
```

Notation:
s[i] shorthand for s.charAt(i).
s[i..] shorthand for s.substring(i).

7

```
// = s but with its blanks removed
public static String deblank(String s) {
    if (s.length == 0)
        return s;
    // {s is not empty}
    if (s.charAt(0) is a blank)
        return deblank(s.substring(1));
    // {s is not empty and s[0] is not a blank}
    return s.charAt(0) +
        deblank(s.substring(1));
}
```

Check the four points:
0. Precise specification?
1. Base case: correct?
2. Recursive case: progress toward termination?
3. Recursive case: correct?

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Check palindrome-hood

A String with at least two characters is a palindrome if
(0) its first and last characters are equal and
(1) chars between first and last form a palindrome:

have to be the same
e.g. AMANAPLANACANALPANAMA
has to be a palindrome

```
/** = "s is a palindrome" */
public static boolean isPal(String s) {
    if (s.length() <= 1)
        return true;
    // { s has at least two characters }
    return s.charAt(0) == s.charAt(s.length()-1) &&
        isPal(s.substring(1, s.length()-1));
}
```

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A man, a plan, a caret, a ban, a myriad, a sum, a lac, a liar, a hoop, a pint, a catalpa, a gas, an oil, a bird, a yell, a vat, a caw, a pax, a wag, a tax, a nay, a ram, a cap, a yam, a gay, a tsar, a wall, a car, a luger, a ward, a bin, a woman, a vassal, a wolf, a tuna, a nit, a pall, a fret, a watt, a bay, a daub, a tan, a cab, a datum, a gall, a hat, a fag, a zap, a say, a jaw, a lay, a wet, a gallop, a tug, a trot, a trap, a tram, a torr, a caper, a top, a tonk, a toll, a ball, a fair, a sax, a minim, a tenor, a bass, a passer, a capital, a rut, an amen, a ted, a cabal, a tang, a sun, an ass, a maw, a sag, a jam, a dam, a sub, a salt, an axon, a sail, an ad, a wadi, a radian, a room, a rood, a rip, a tad, a pariah, a revel, a reel, a reed, a pool, a plug, a pin, a peck, a parabola, a dog, a pat, a cud, a nu, a fan, a pal, a rum, a nod, an eta, a lag, an eel, a batik, a mug, a mot, a nap, a maxim, a mood, a leek, a grub, a gob, a gel, a drab, a citadel, a total, a cedar, a tap, a gag, a rat, a manor, a bar, a gal, a cola, a pap, a yaw, a tab, a raj, a gab, a nag, a pagan, a bag, a jar, a bat, a way, a papa, a local, a gar, a baron, a mat, a rag, a gap, a tar, a decal, a tot, a led, a tic, a bard, a leg, a bog, a burg, a keel, a doom, a mix, a map, an atom, a gum, a kit, a baleen, a gala, a ten, a don, a mural, a pan, a faun, a ducat, a pagoda, a lob, a rap, a keep, a nip, a gulp, a loop, a deer, a leer, a lever, a hair, a pad, a tapir, a door, a moor, an aid, a raid, a wad, an alias, an ox, an atlas, a bus, a madam, a jag, a saw, a mass, an anus, a gnat, a lab, a cadet, an em, a natural, a tip, a caress, a pass, a baronet, a minimax, a sari, a fall, a ballot, a knot, a pot, a rep, a carrot, a mart, a part, a tort, a gut, a poll, a gateway, a law, a jay, a sap, a zag, a fat, a hall, a gamut, a dab, a can, a tabu, a day, a batt, a waterfall, a patina, a nut, a flow, a lass, a van, a mow, a nib, a draw, a regular, a call, a war, a stay, a gam, a yap, a cam, a ray, an ax, a tag, a wax, a paw, a cat, a valley, a drib, a lion, a saga, a plat, a catnip, a pooh, a rail, a calamus, a dairyman, a bater, a canal ---Panama!

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Tiling Elaine's kitchen

Elaine has a 2^n by 2^n kitchen. One square of it is covered by a 1 by 1 refrigerator. Tile the kitchen with these kinds of tiles:

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Tiling Elaine's kitchen

```
/** tile a 2^n by 2^n kitchen with 1 square filled. */
public static void tile(int n) {
    if ( )
}
}
```

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