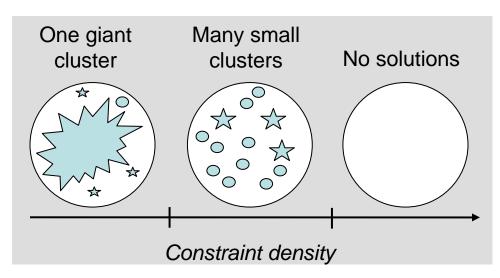
Counting Solution Clusters in Graph Coloring Problems Using Belief Propagation

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Known facts:

- Solution space of random combinatorial problems fractures into clusters as constraint density (& hardness) increases
- The fastest solution technique relies on marginal probability estimates over clusters



= cluster of satisfying assignments

= trap (almost satisfying)

Our results:

 An expression to count the number of clusters with high precision

$$Z_{(-1)} = \sum_{\vec{y} \in DomExt^n} \left(-1 \right)^{\#e(\vec{y})} \prod_{\alpha} f_{\alpha}(\vec{y}_{\alpha})$$

 A message-passing scheme similar to BP that approximates Z₍₋₁₎ well

